

UpProver Tool: Incremental Verification by SMT-based Summary Repair



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How to (improve scalability)² ?

Software passes through small frequent changes (re-verification is impractical)

Improving scalability by:

- 1) **Avoiding repetition** in analysis of closely-related program versions (e.g., Incremental verification)
- 2) Leveraging success of **SMT** (e.g., word-level vs. bit-blasting)

Our take:

- **Reusing** efforts from one verification run to another:
 - Function Summarization based on Craig interpolation
- **SMT**-encoding and reasoning

Context

Software Bounded Model Checking [Biere et al. 1999, Clarke et al. 2004]

- Loops/recursion unrolled up to a predefined bound

Program encoded into a symbolic **BMC formula**

- Via constructing a Static Single Assignment Form

BMC formula conjoined with the negation of **assertions**

- To encode undesired behaviors

Satisfiability check by a SAT/SMT-solver

UNSAT → Bounded program is **safe**



SAT → Error found (Satisfying assignment identifies an error trace)



Need for theory reasoning

Need for theory reasoning

version1.c

```
int a, b, c;
int func() {
    c = b;
    if (a > 0)
        a = b;
    int i, m = 0;
    for (i = 0; i < 100; i++)
        m += a*b;
    return m;
}
void main() {
    a=nondet(); b=nondet();
    if (a <= 0) return -1;
    b = func();
    assert(a == c);

    int p = func();
    int q = func();
    assert(p == q);
}
```

Need for theory reasoning

version1.c

```
int a, b, c;
int func() {
    c = b;
    if (a > 0)
        a = b;
    int i, m = 0;
    for (i = 0; i < 100; i++)
        m += a*b;
    return m;
}
void main() {
    a=nondet(); b=nondet();
    if (a <= 0) return -1;
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version1.c



```
int a, b, c;
int func() {
    c = b;
    if (a > 0)
        a = b;
    int i, m = 0;
    for (i = 0; i < 100; i++)
        m += a*b;
    return m;
}
void main() {
    a=nondet(); b=nondet();
    if (a <= 0) return -1;
    b = func();
    assert(a == c);

    int p = func();
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    assert(p == q);
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```

Need for theory reasoning

version1.c

```
int a, b, c;
int func() {
    c = b;
    if (a > 0)
        a = b;
    int i, m = 0;
    for (i = 0; i < 100; i++)
        m += a*b;
    return m;
}
```

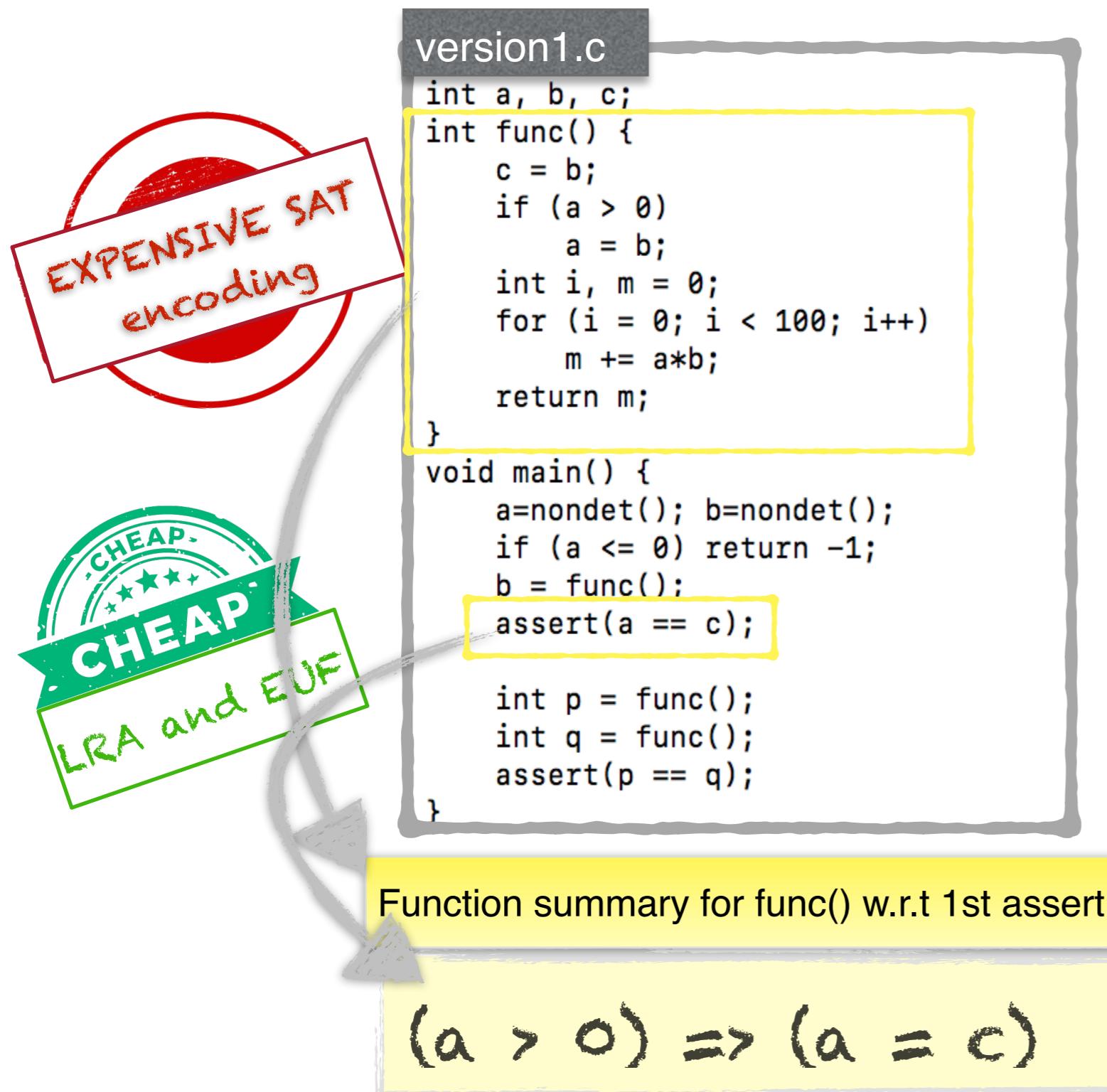
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```

EXPENSIVE SAT
encoding

CHEAP
CHEAP
LRA and EUF

Need for theory reasoning



Need for theory reasoning

version1.c

```
int a, b, c;
int func() {
    c = b;
    if (a > 0)
        a = b;
    int i, m = 0;
    for (i = 0; i < 100; i++)
        m += a*b;
    return m;
}
void main() {
    a=nondet(); b=nondet();
    if (a <= 0) return -1;
    b = func();
    assert(a == c);

    int p = func();
    int q = func();
    assert(p == q);
}
```

EXPENSIVE SAT
encoding

CHEAP
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LRA and EUF

version2.c

```
int a, b, c;
int func() {
    c = b;
    if (a > 0)
        a = b;
    int i, m = 0;
    for (i = 0; i < 100; i++)
        m += a*b;
    return m + 1;
}
void main() {
    a=nondet(); b=nondet();
    if (a <= 0) return -1;
    b = func();
    assert(a == c);

    int p = func();
    int q = func();
    assert(p == q);
}
```

Function summary for func() w.r.t 1st assert

$$(a > 0) \Rightarrow (a = c)$$

Need for theory reasoning

version1.c

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int a, b, c;
int func() {
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    if (a > 0)
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        m += a*b;
    return m;
}
void main() {
    a=nondet(); b=nondet();
    if (a <= 0) return -1;
    b = func();
    assert(a == c); ✓ safe

    int p = func();
    int q = func();
    assert(p == q);
}
```

EXPENSIVE SAT
encoding

CHEAP
CHEAP

LRA and EUF

version2.c

```
int a, b, c;
int func() {
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    if (a > 0)
        a = b;
    int i, m = 0;
    for (i = 0; i < 100; i++)
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    return m + 1;
}
void main() {
    a=nondet(); b=nondet();
    if (a <= 0) return -1;
    b = func();
    assert(a == c); safe ??

    int p = func();
    int q = func();
    assert(p == q);
}
```

Function summary for func() w.r.t 1st assert

$$(a > 0) \Rightarrow (a = c)$$

Is this summary good enough
to over-approximate the
function after change?

The UpProver tool

A BMC tool, incrementally verifies program versions in C

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A BMC tool, incrementally verifies program versions in C

In contrast to its predecessor, a SAT-based tool eVOLCHECK:



- ✓ UpProver offers two more levels of SMT-encoding:
 - Equality Logic & Uninterpreted Functions (**EUF**)
 - Linear Real Arithmetic (**LRA**)
- ✓ UpProver leverages tree-interpolation systems in SMT to localize and speed up the checks of new versions
- ✓ UpProver offers a trade-off between precision and performance
- ✓ UpProver performs an automated summary **repair**

Function Summarization

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- A technique to create and reuse over-approximation of the function behavior

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- A technique to create and reuse over-approximation of the function behavior
- Expressed using function's in/out parameters
- Contains only the relevant information to prove properties

Function Summarization

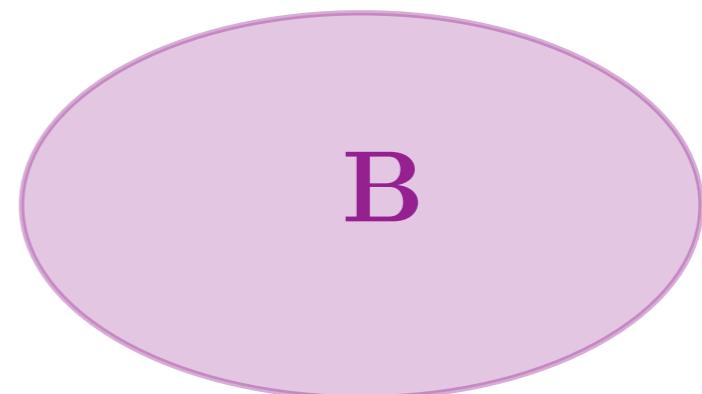
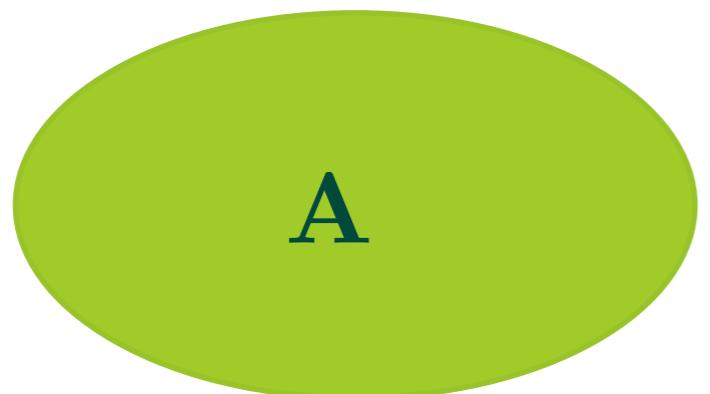
- A technique to create and reuse over-approximation of the function behavior
- Expressed using function's in/out parameters
- Contains only the relevant information to prove properties
- Summary is derived by **Craig interpolation** after SMT-solver returns UNSAT

Craig interpolation [Craig'57]

abstraction from proof

Given mutually unsatisfiable formulas A and B , an **interpolant** is a formula I such that

- $A \rightarrow I$
- $I \wedge B$ is unsatisfiable
- I is defined over common symbols of A and B

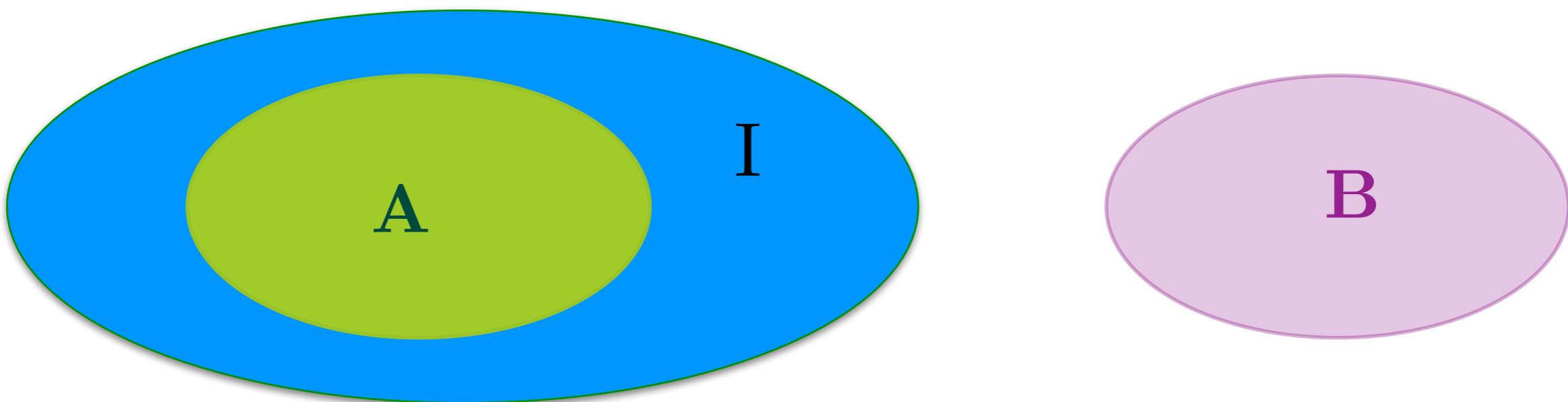


Craig interpolation [Craig'57]

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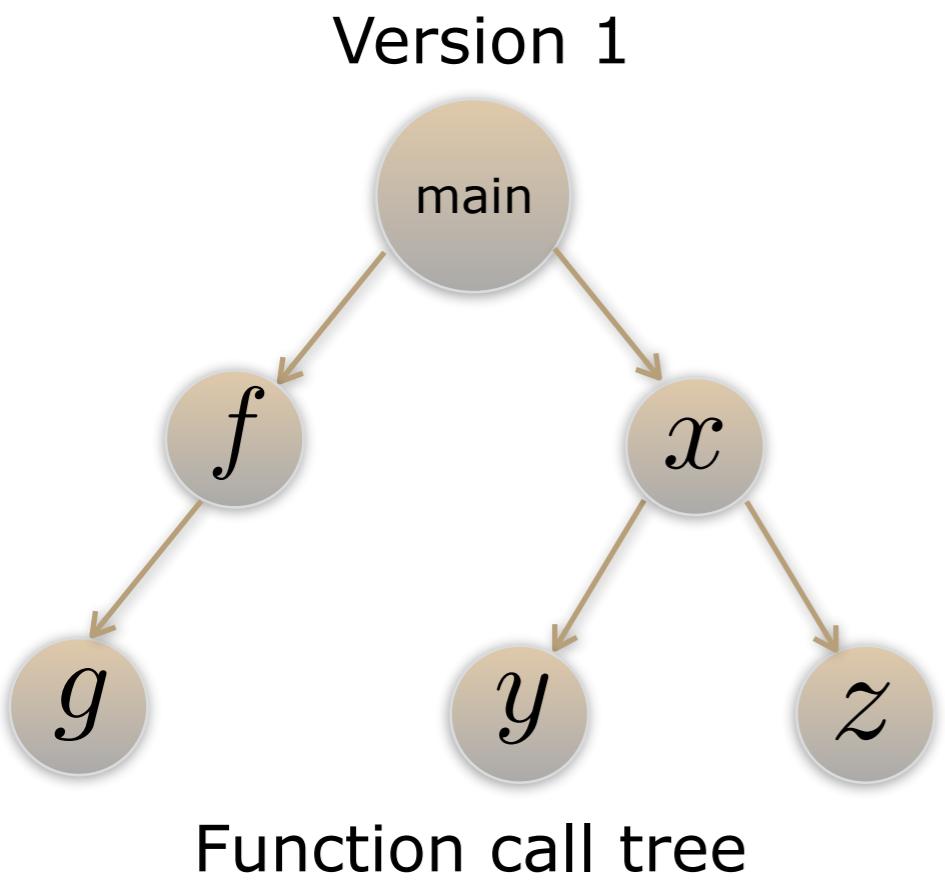
- $A \rightarrow I$
- $I \wedge B$ is unsatisfiable
- I is defined over common symbols of A and B

To guarantee the algorithmic correctness of
UpProver, tree-interpolation property is required.

For more details see

“Farkas-Based Tree Interpolation”, [Asadi et al. SAS’20]

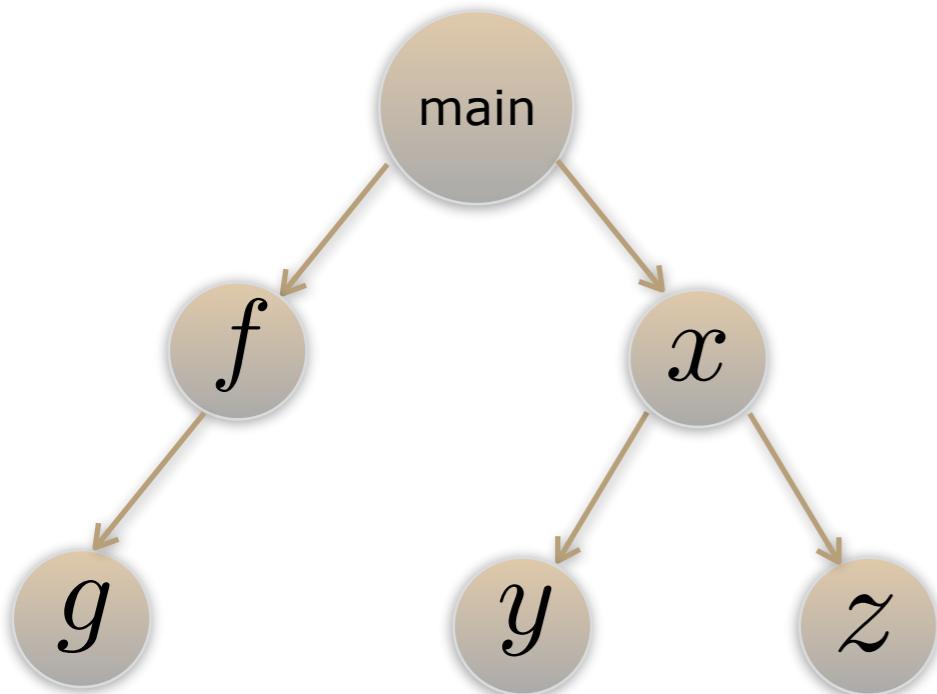
Bootstrap verification



Bootstrap verification

$$\varphi_g \wedge \varphi_f \wedge \varphi_{main} \wedge \varphi_y \wedge \varphi_x \wedge \varphi_z \wedge error$$

Version 1

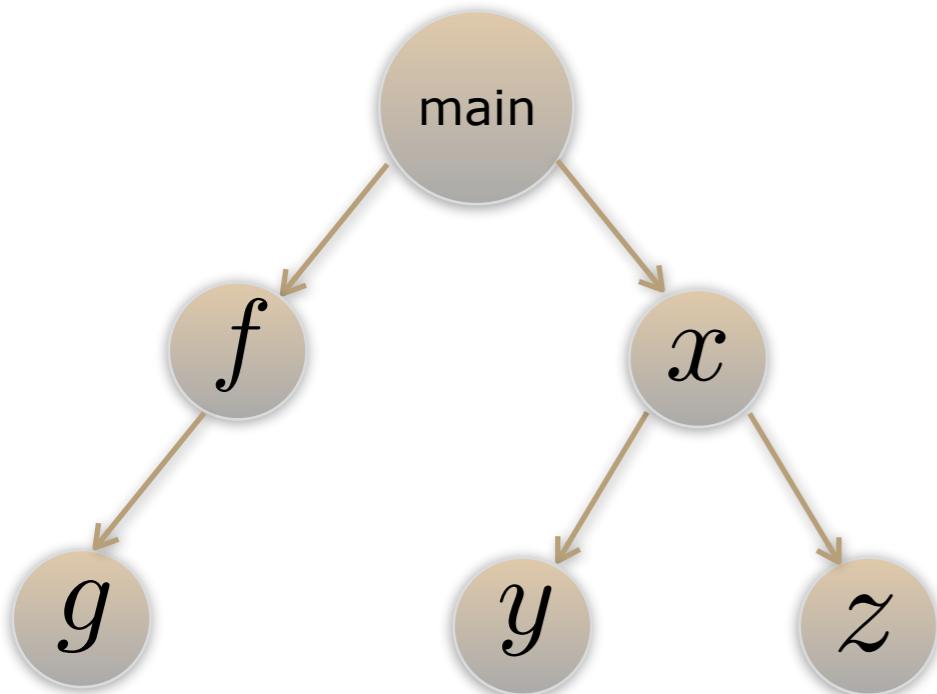


Function call tree

Bootstrap verification

$\varphi_g \wedge \varphi_f \wedge \varphi_{main} \wedge \varphi_y \wedge \varphi_x \wedge \varphi_z \wedge error \rightarrow UNSAT \checkmark$

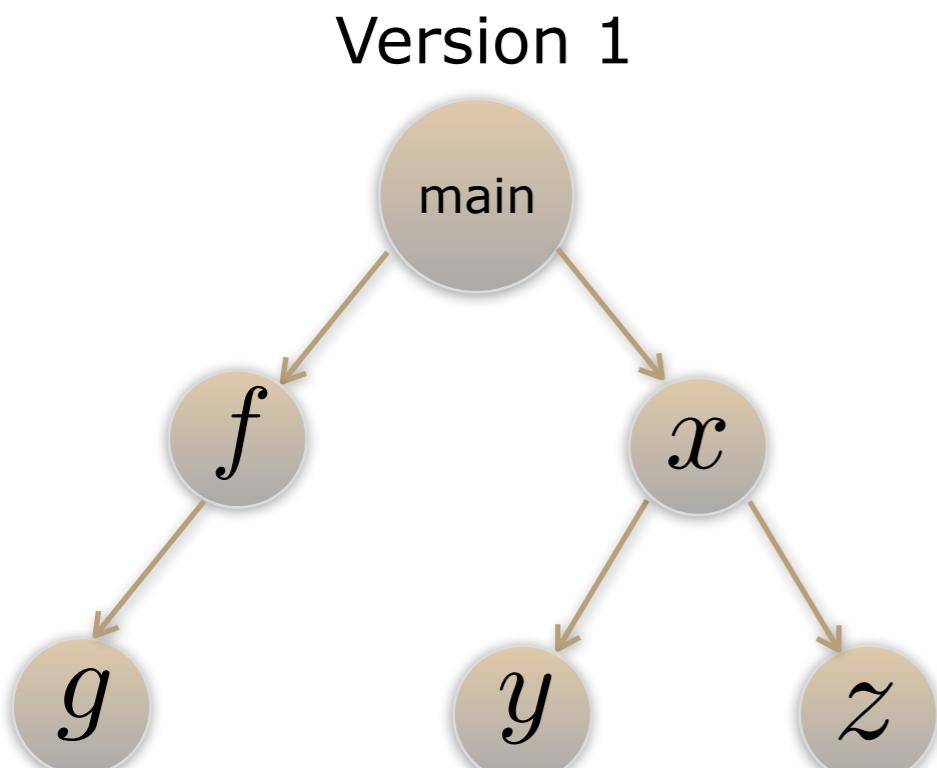
Version 1



Function call tree

Bootstrap verification

$\varphi_g \wedge \varphi_f \wedge \varphi_{main} \wedge \varphi_y \wedge \varphi_x \wedge \varphi_z \wedge error$ UNSAT



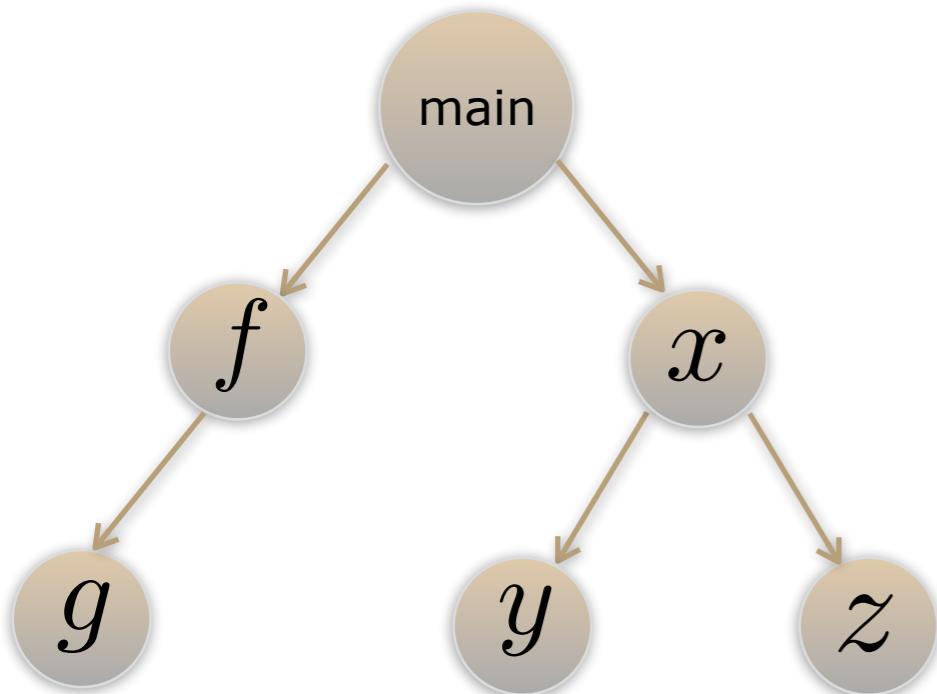
Function call tree

Bootstrap verification

$$\varphi_g \wedge \varphi_f \wedge \varphi_{main} \wedge \varphi_y \wedge \varphi_x \wedge \varphi_z \wedge error \rightarrow \text{UNSAT} \quad \checkmark$$

$\varphi_g \wedge \varphi_f \wedge \varphi_{main} \wedge \varphi_y \wedge \varphi_x \wedge \varphi_z \wedge error$ is grouped by a purple brace under S_g .

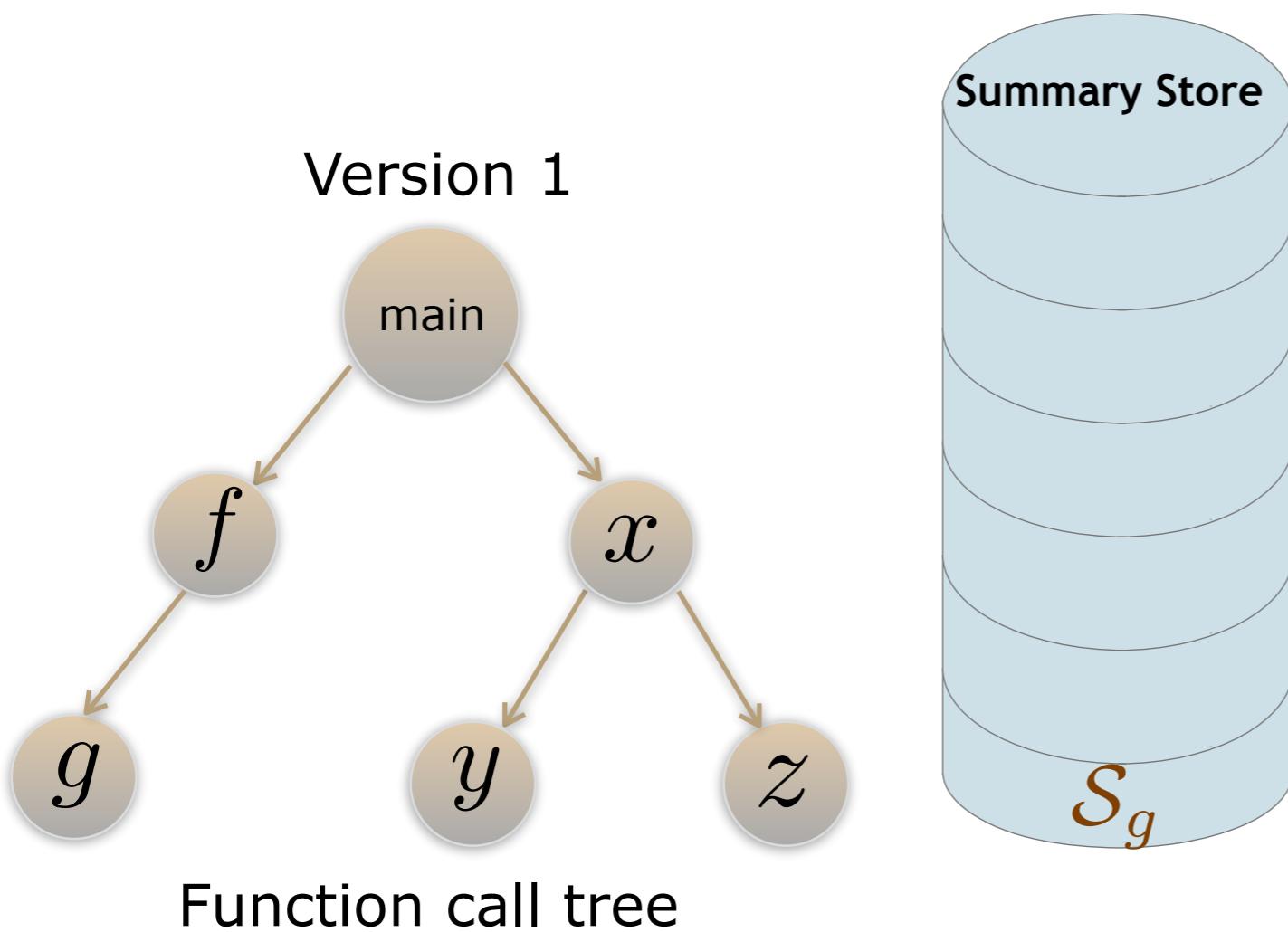
Version 1



Function call tree

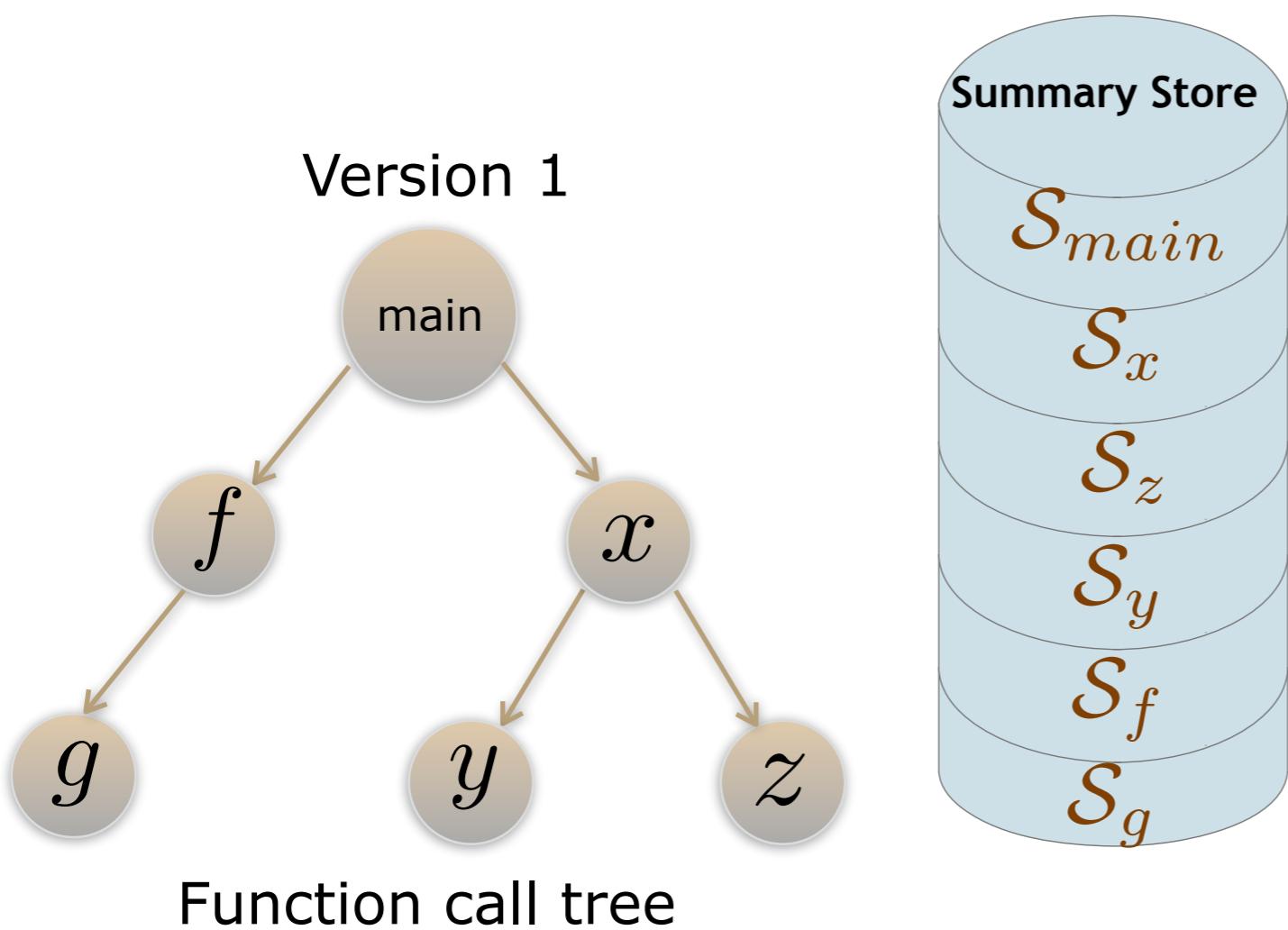
Bootstrap verification

$\varphi_g \wedge \varphi_f \wedge \varphi_{main} \wedge \varphi_y \wedge \varphi_x \wedge \varphi_z \wedge error$  UNSAT 



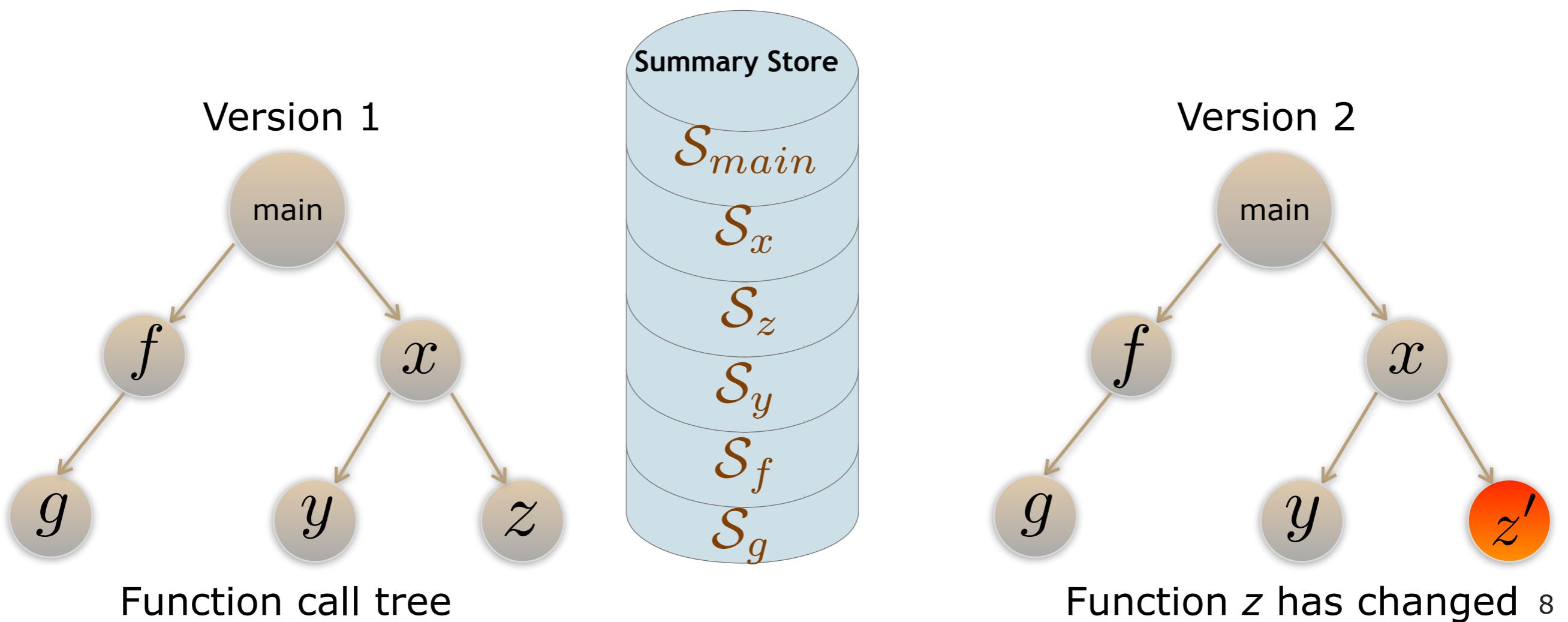
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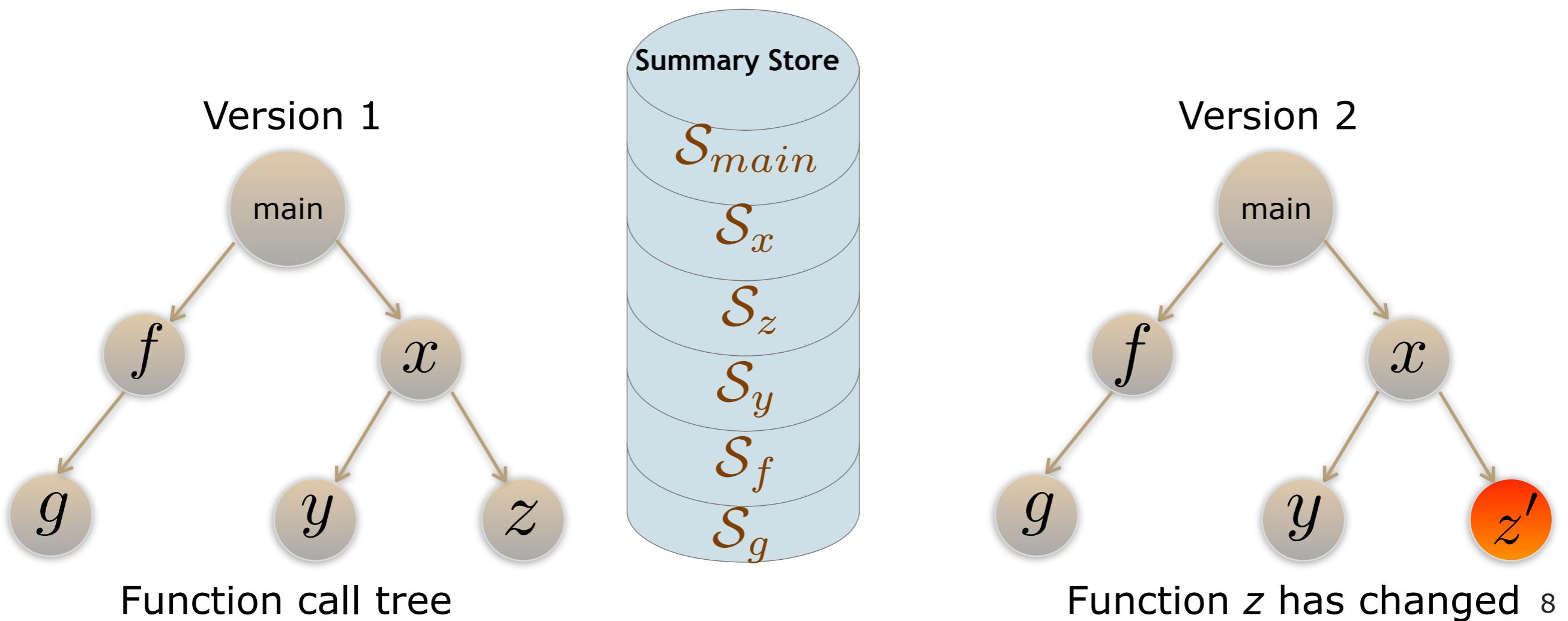
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Bootstrap verification

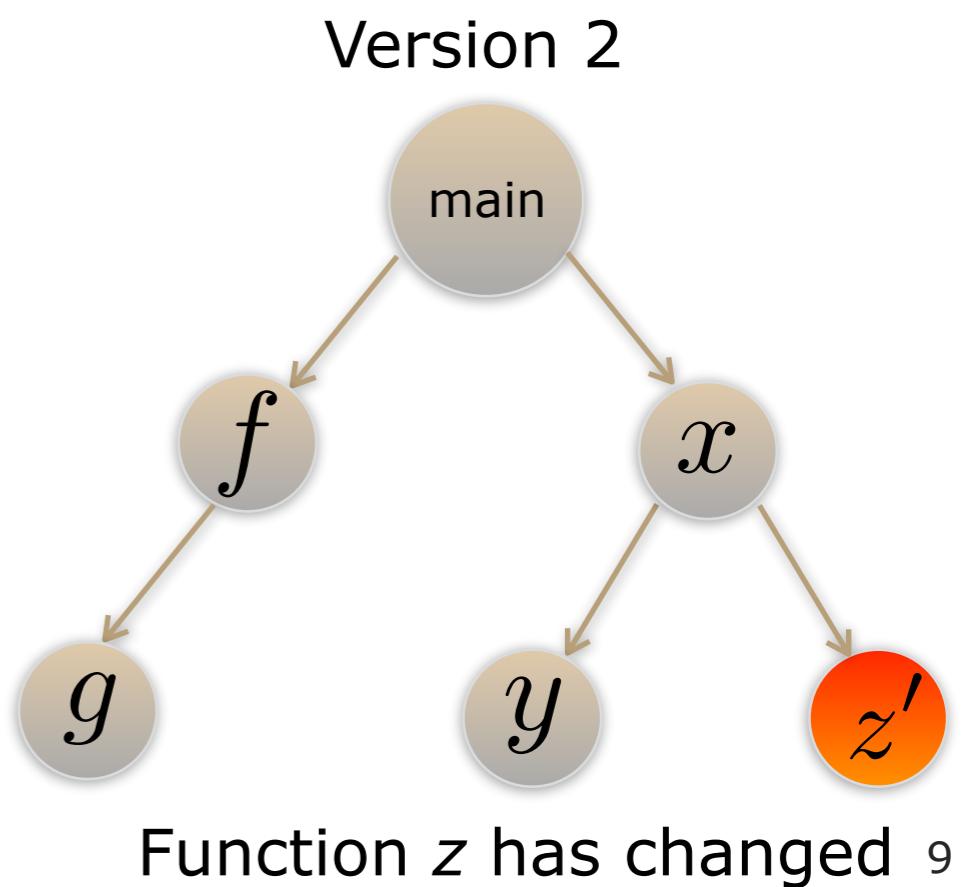
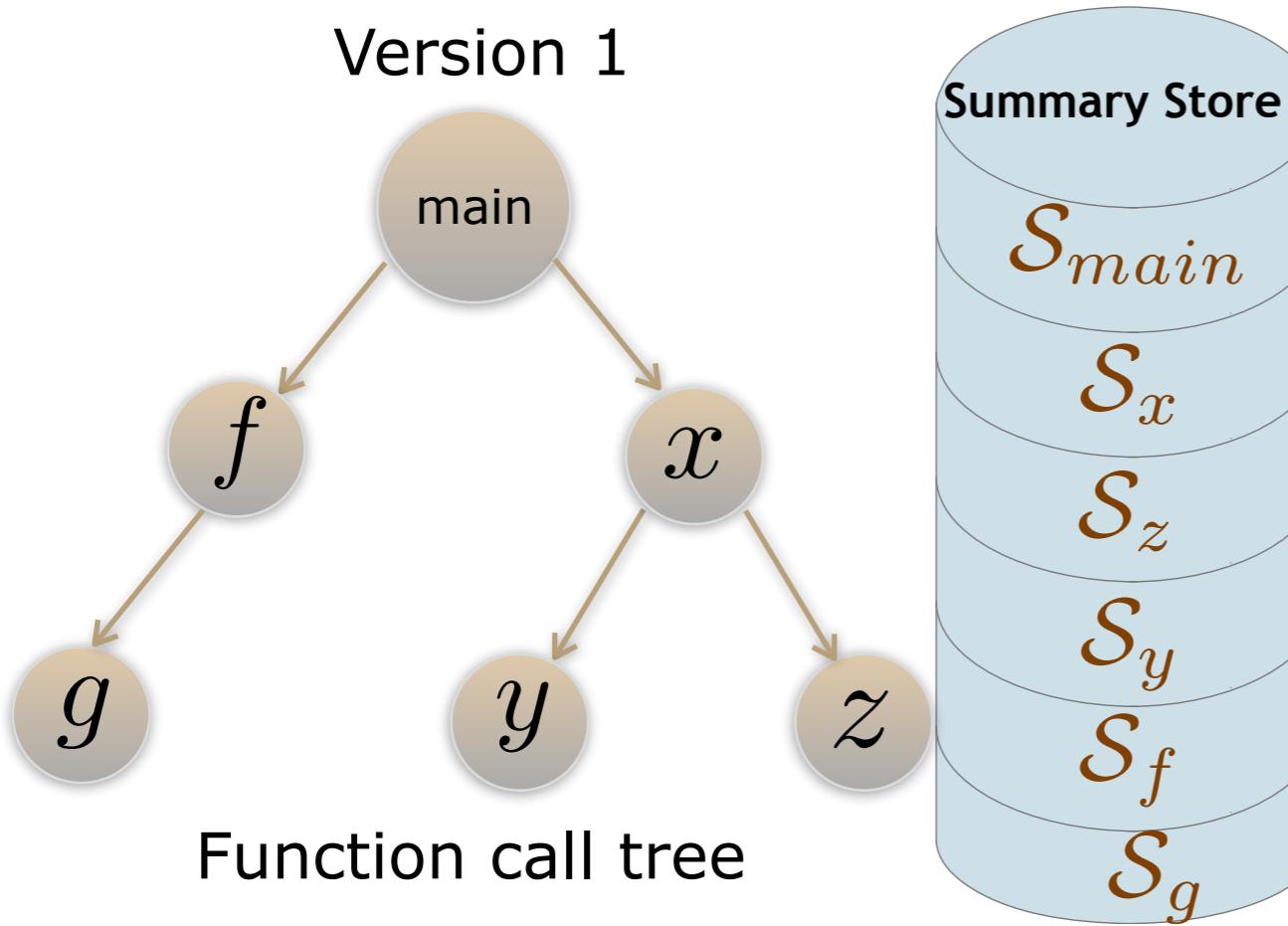
We try to check if summary S_z is still a valid over-approximation of z'



Incremental verification

Validating \mathcal{S}_z :

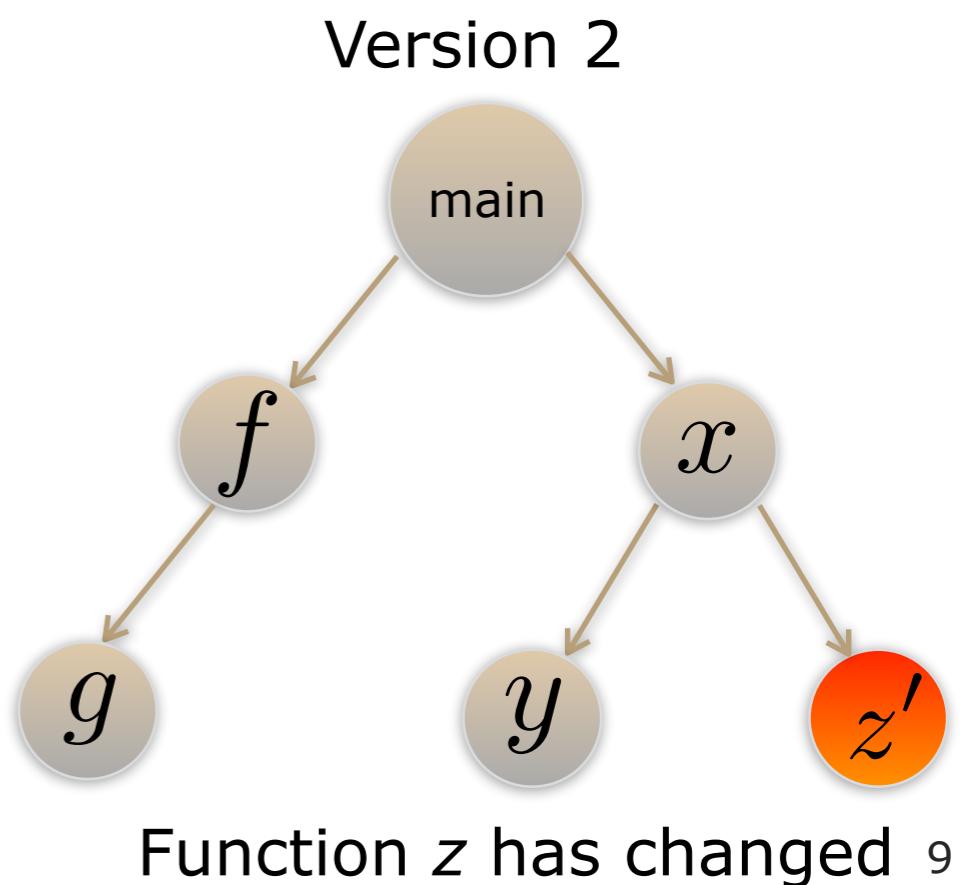
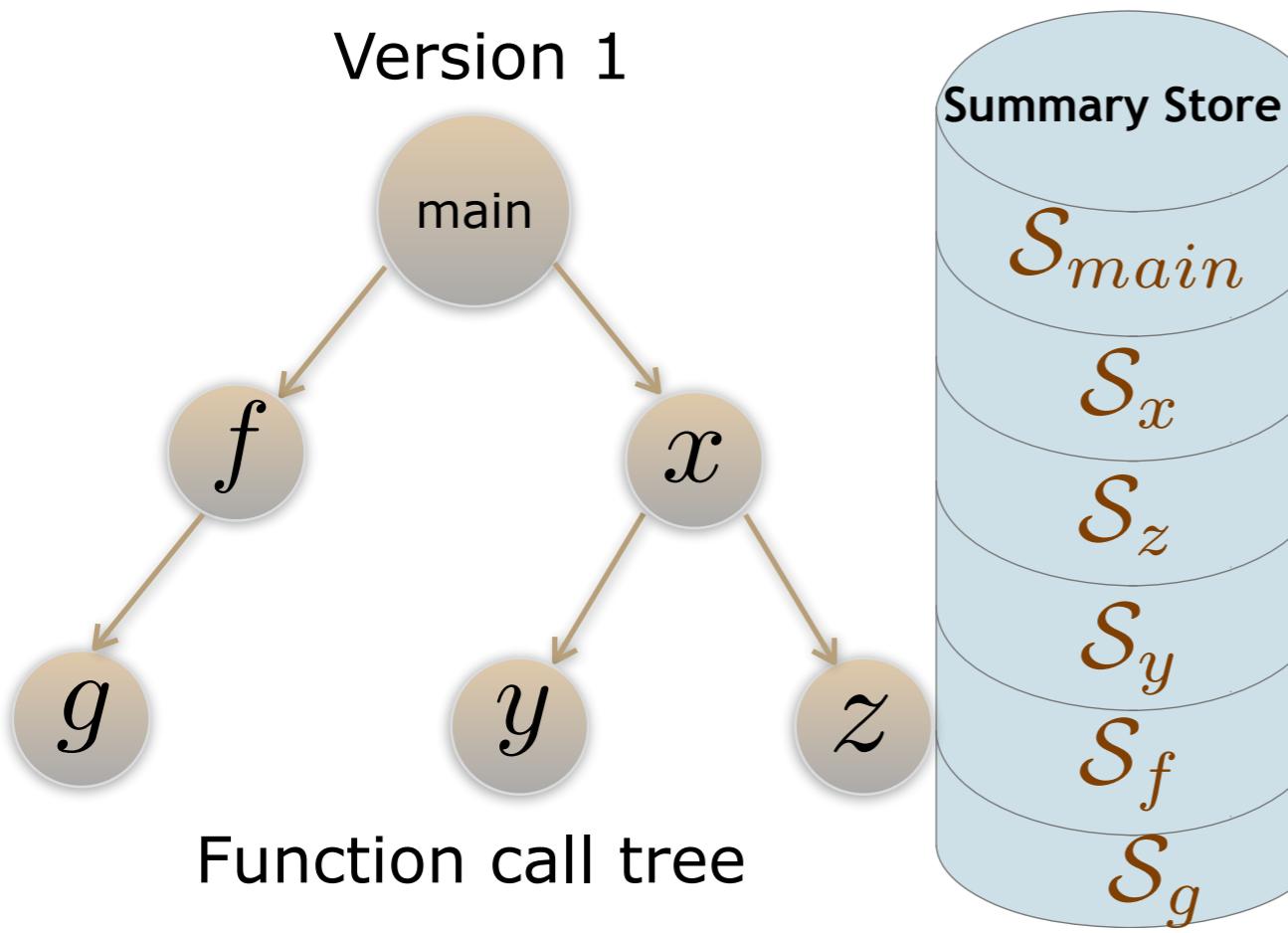
$$\varphi_{z'} \implies \mathcal{S}_z$$



Incremental verification

Validating \mathcal{S}_z :

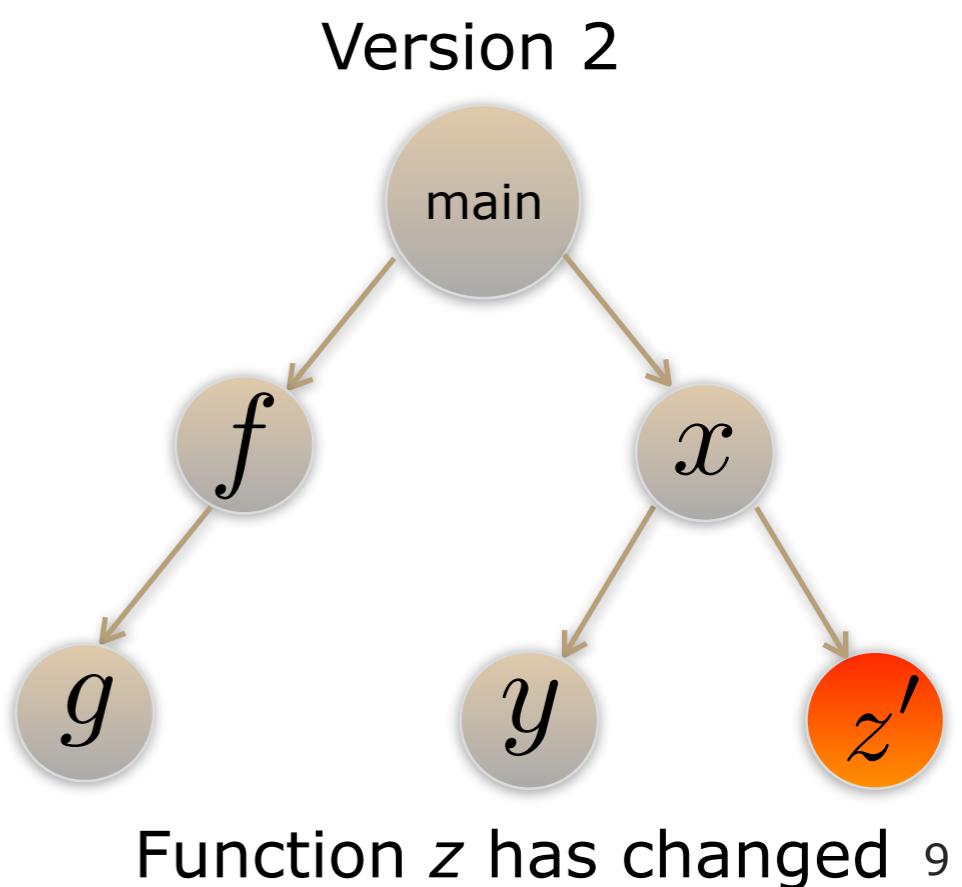
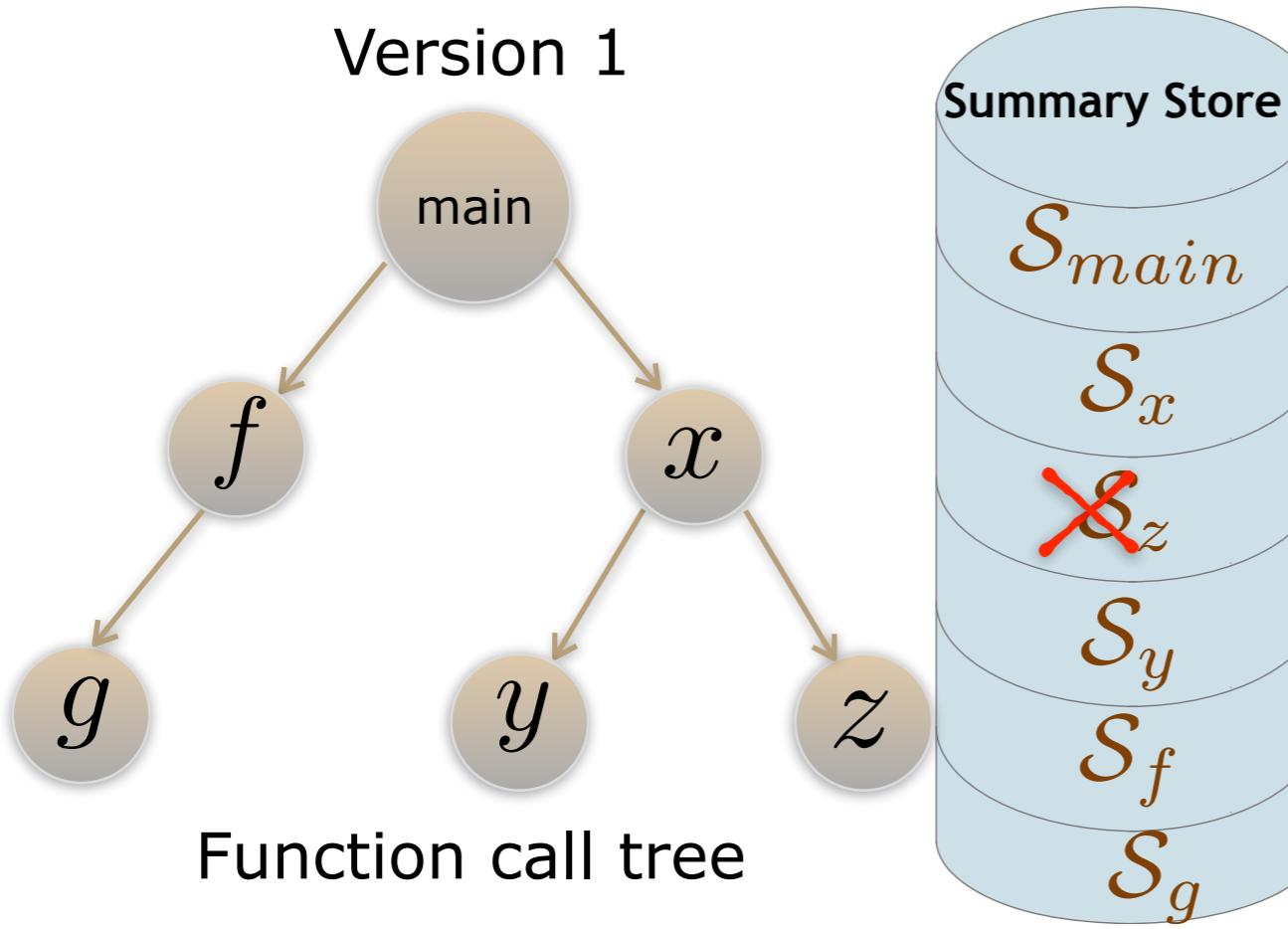
$$\varphi_{z'} \implies \mathcal{S}_z \times \text{Invalid, Propagate upwards}$$



Incremental verification

Validating \mathcal{S}_z :

$\varphi_{z'} \implies \mathcal{S}_z \times \text{Invalid, Propagate upwards}$

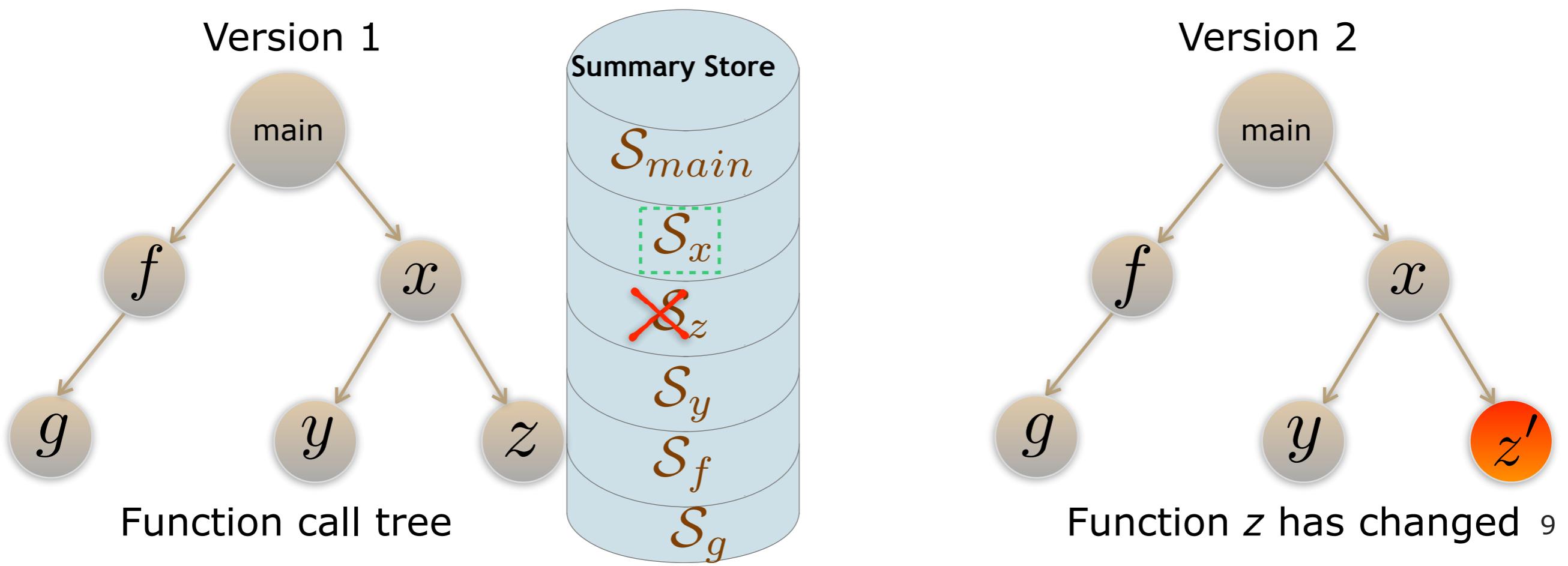


Incremental verification

Validating \mathcal{S}_z :

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Validating \mathcal{S}_x :



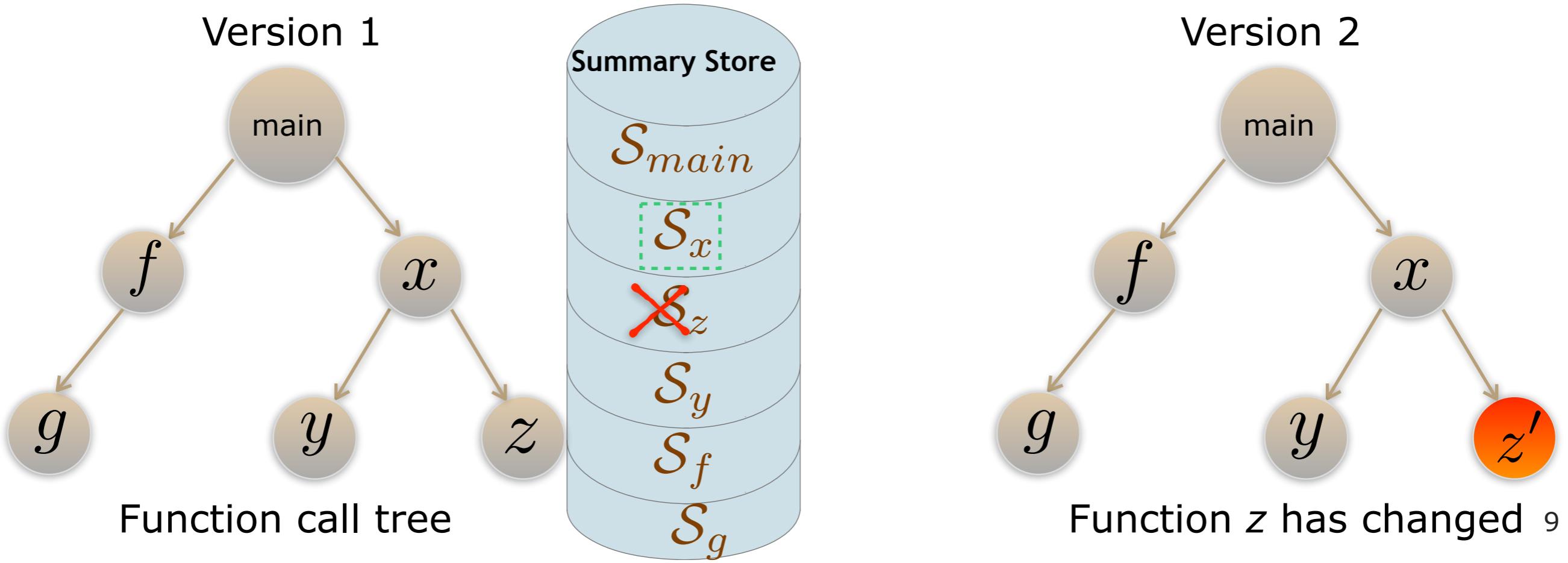
Incremental verification

Validating \mathcal{S}_z :

$$\varphi_{z'} \implies \mathcal{S}_z \times \text{Invalid, Propagate upwards}$$

Validating \mathcal{S}_x :

$$\varphi'_z \wedge \mathcal{S}_y \wedge \varphi_x \implies \mathcal{S}_x$$



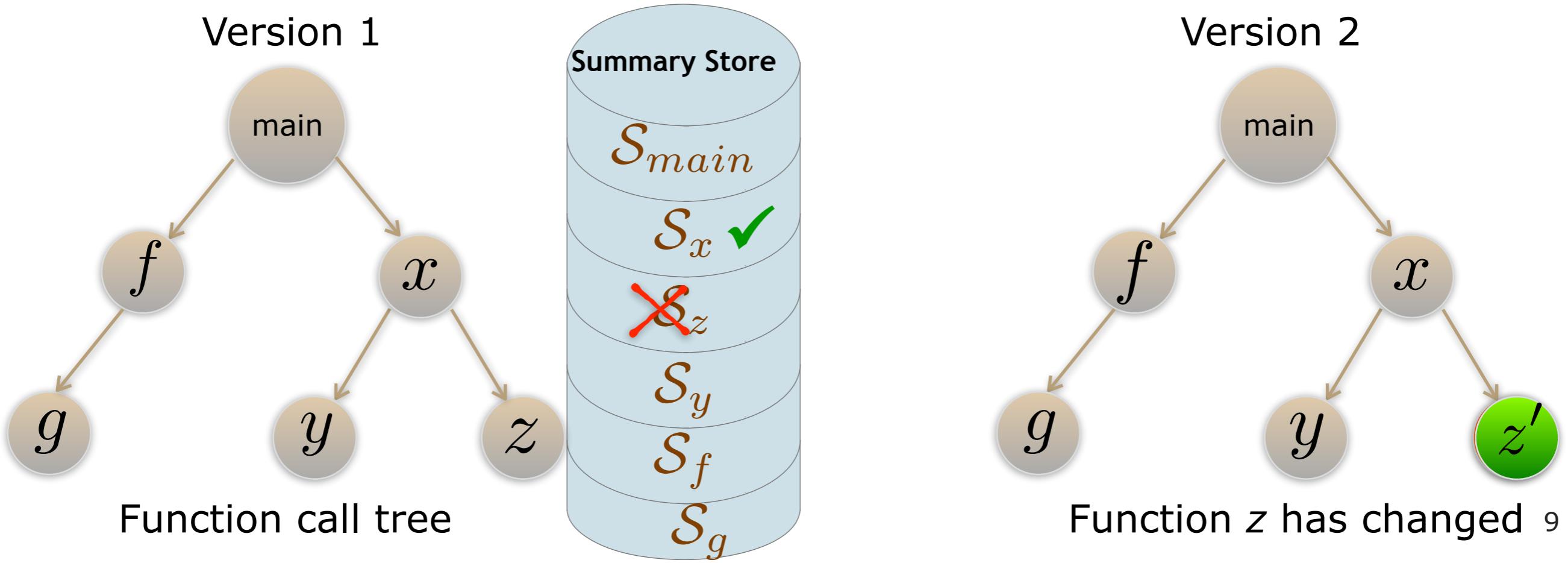
Incremental verification

Validating \mathcal{S}_z :

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Validating \mathcal{S}_x :

$\varphi'_z \wedge \mathcal{S}_y \wedge \varphi_x \implies \mathcal{S}_x \checkmark \text{change is safe}$



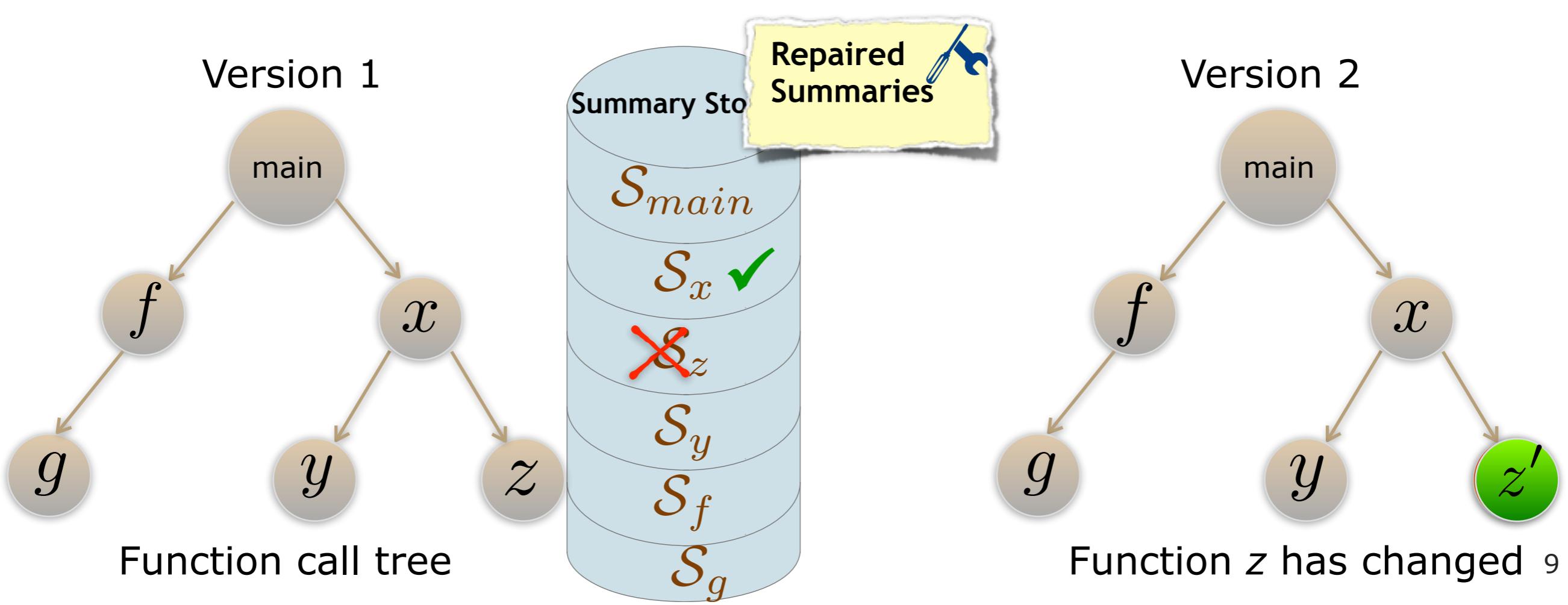
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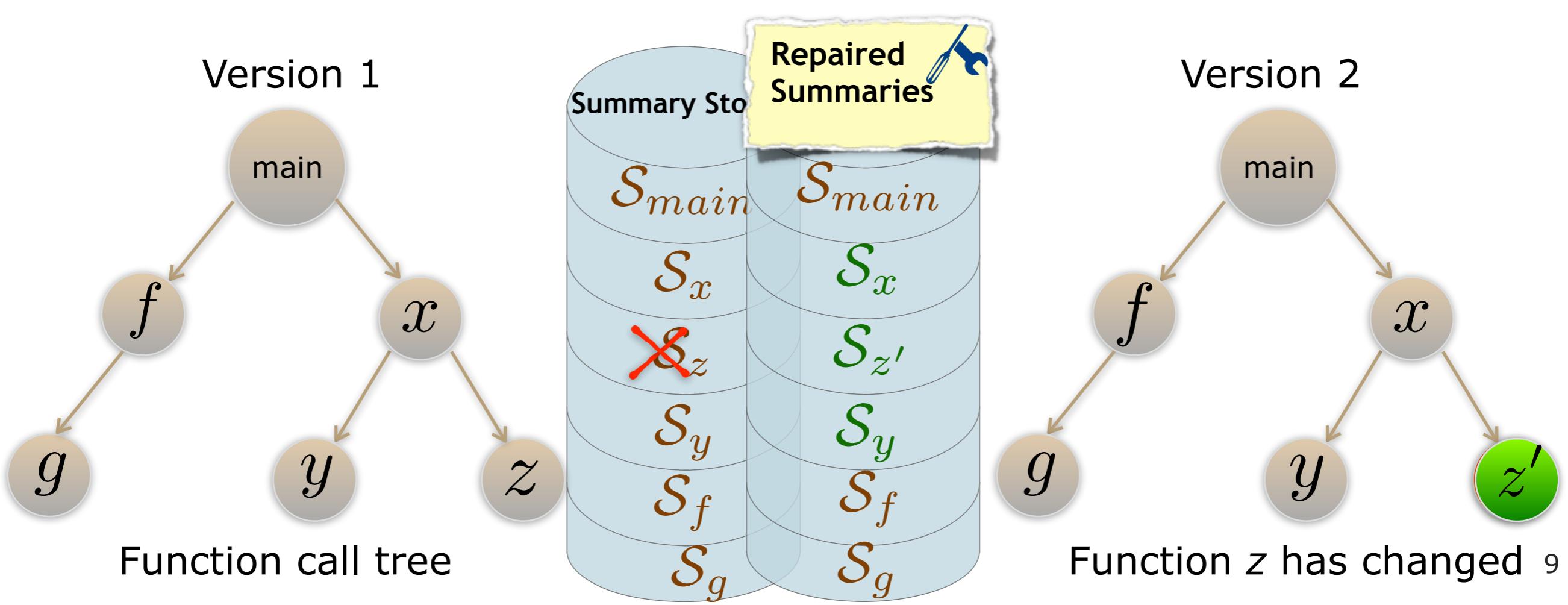
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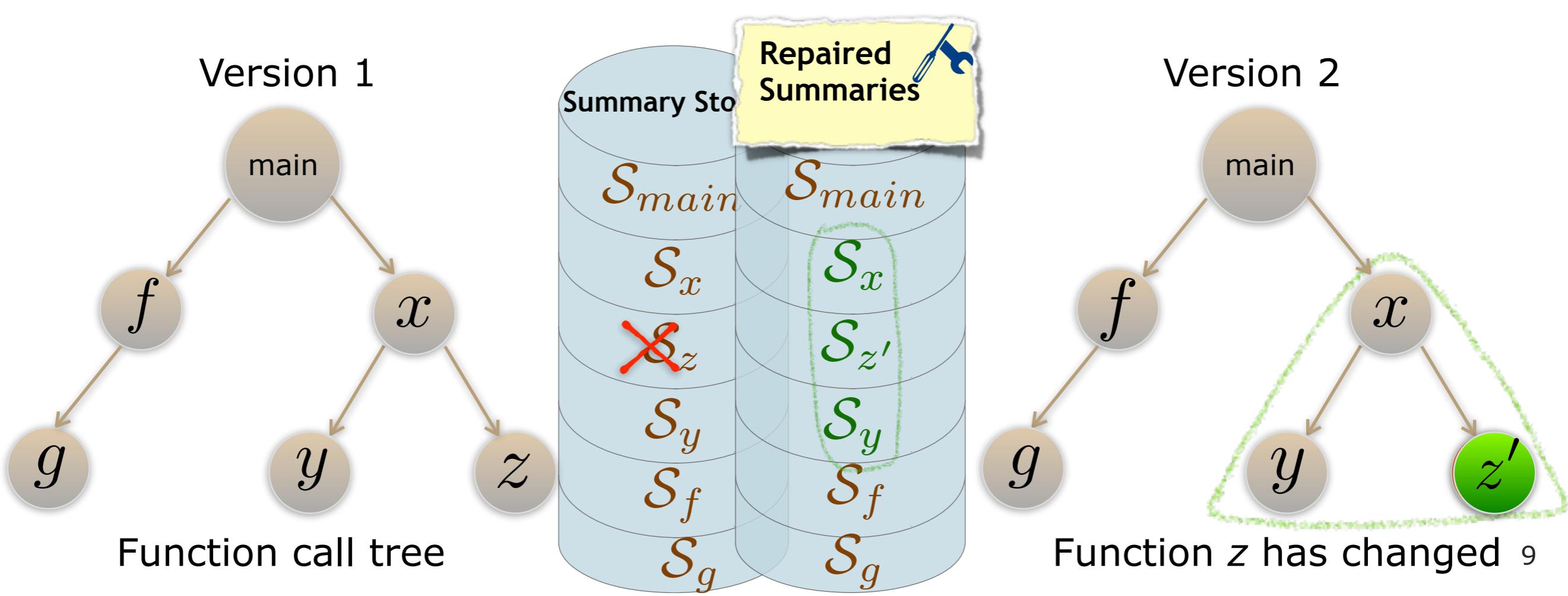
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UpProver's SMT encodings

- Equality Logic & Uninterpreted Functions (**EUF**)
 - Example: $(f(x, y) \neq f(u, v)) \wedge (x = u) \wedge (y = v)$



UpProver's SMT encodings

- ▶ Equality Logic & Uninterpreted Functions (**EUF**)
 - Example: $(f(x, y) \neq f(u, v)) \wedge (x = u) \wedge (y = v)$
- ▶ Linear Real Arithmetic (**LRA**)
 - Example: $(x + y \leq 0) \wedge (x = 0) \wedge (\neg a \vee (x = 1) \vee (y \geq 0))$



UpProver's SMT encodings

- Equality Logic & Uninterpreted Functions (**EUF**)



- Example: $(f(x, y) \neq f(u, v)) \wedge (x = u) \wedge (y = v)$

- Linear Real Arithmetic (**LRA**)

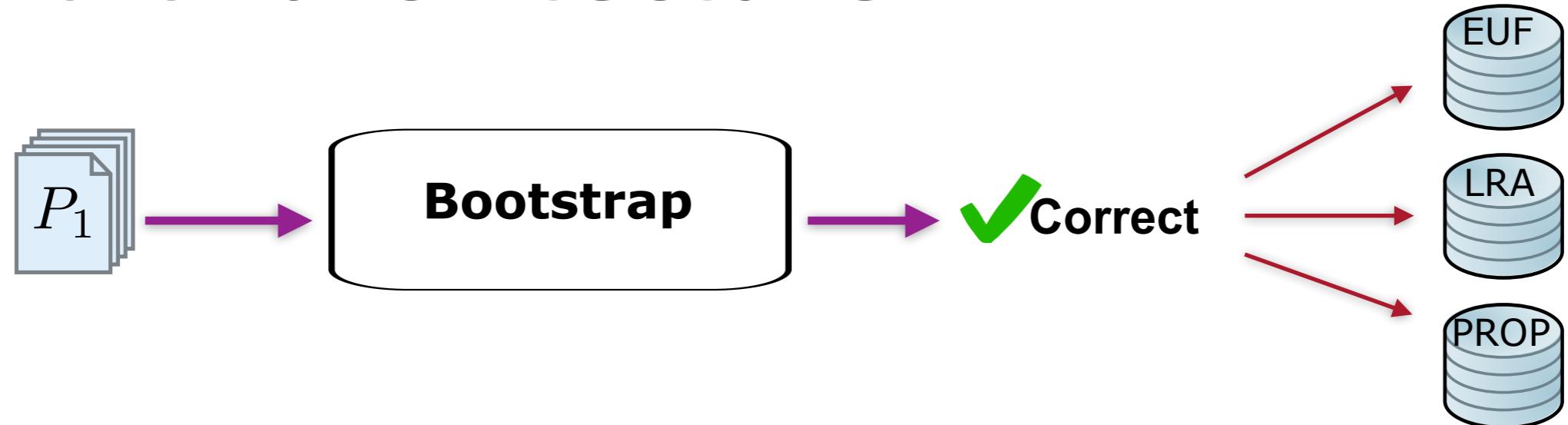
- Example: $(x + y \leq 0) \wedge (x = 0) \wedge (\neg a \vee (x = 1) \vee (y \geq 0))$

- Propositional Logic (**Prop**)

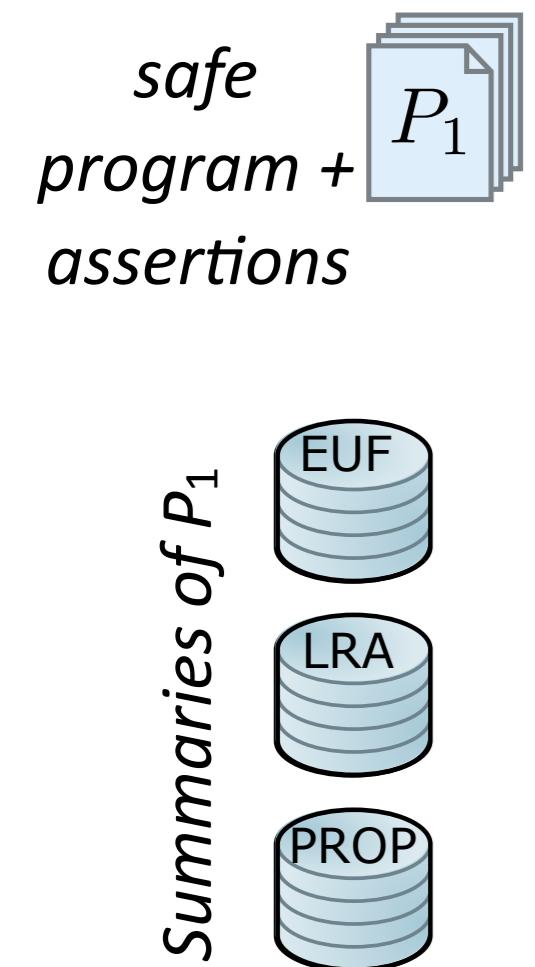
- Example: $\left[(a + b) \% 2 \neq ((a \% 2) + (b \% 2)) \% 2 \right]$



UpProver architecture



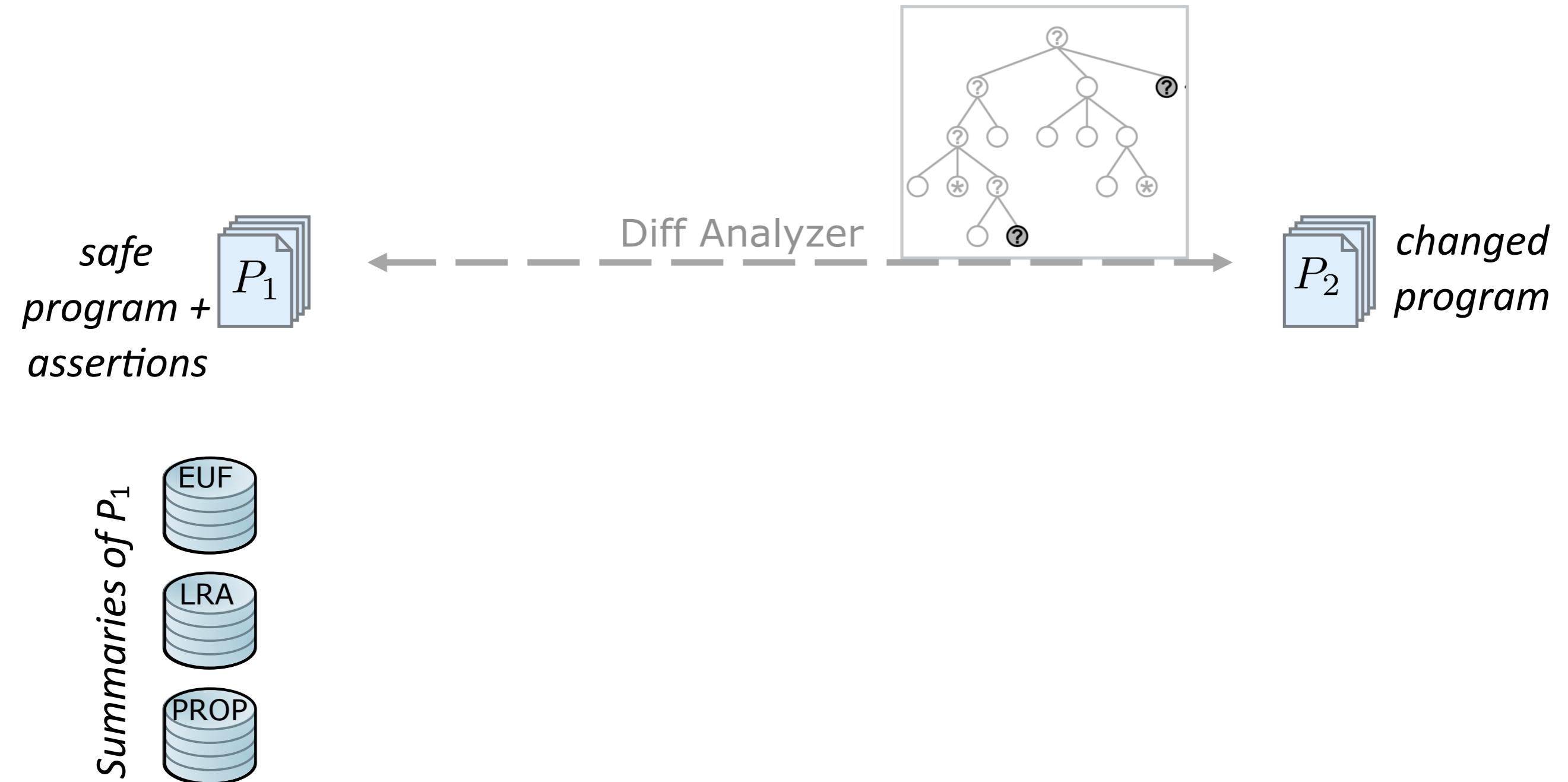
UpProver architecture



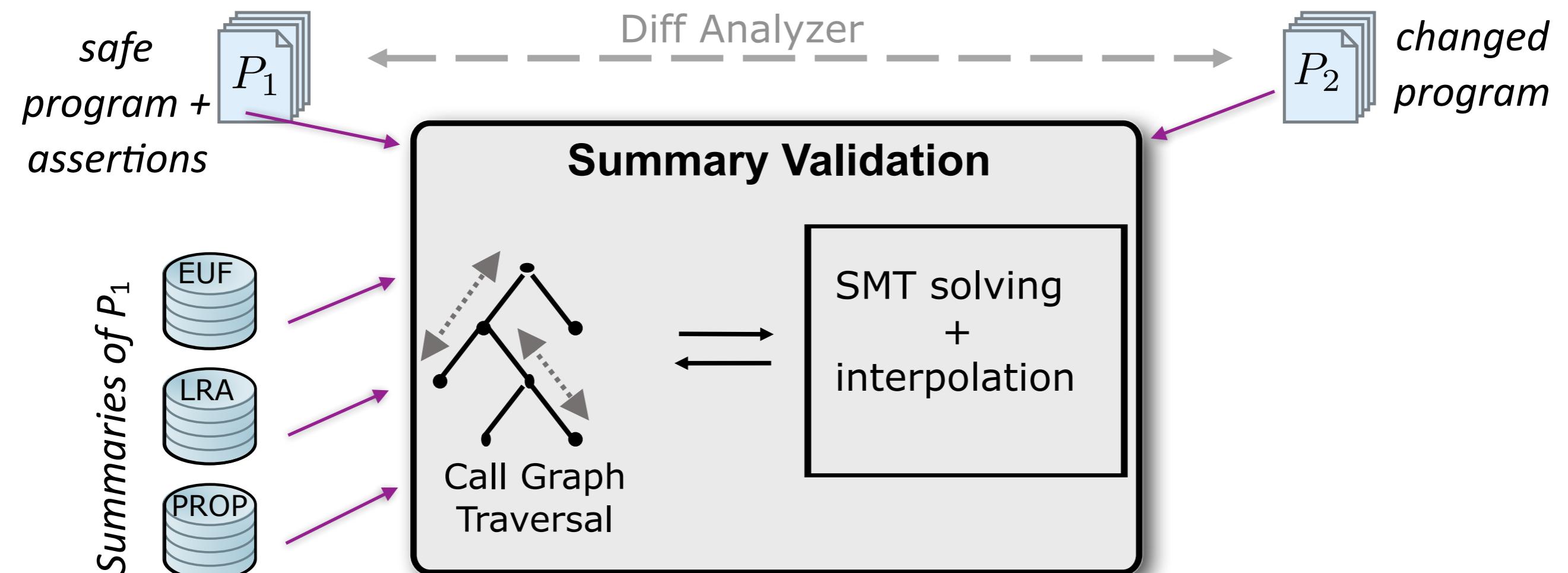
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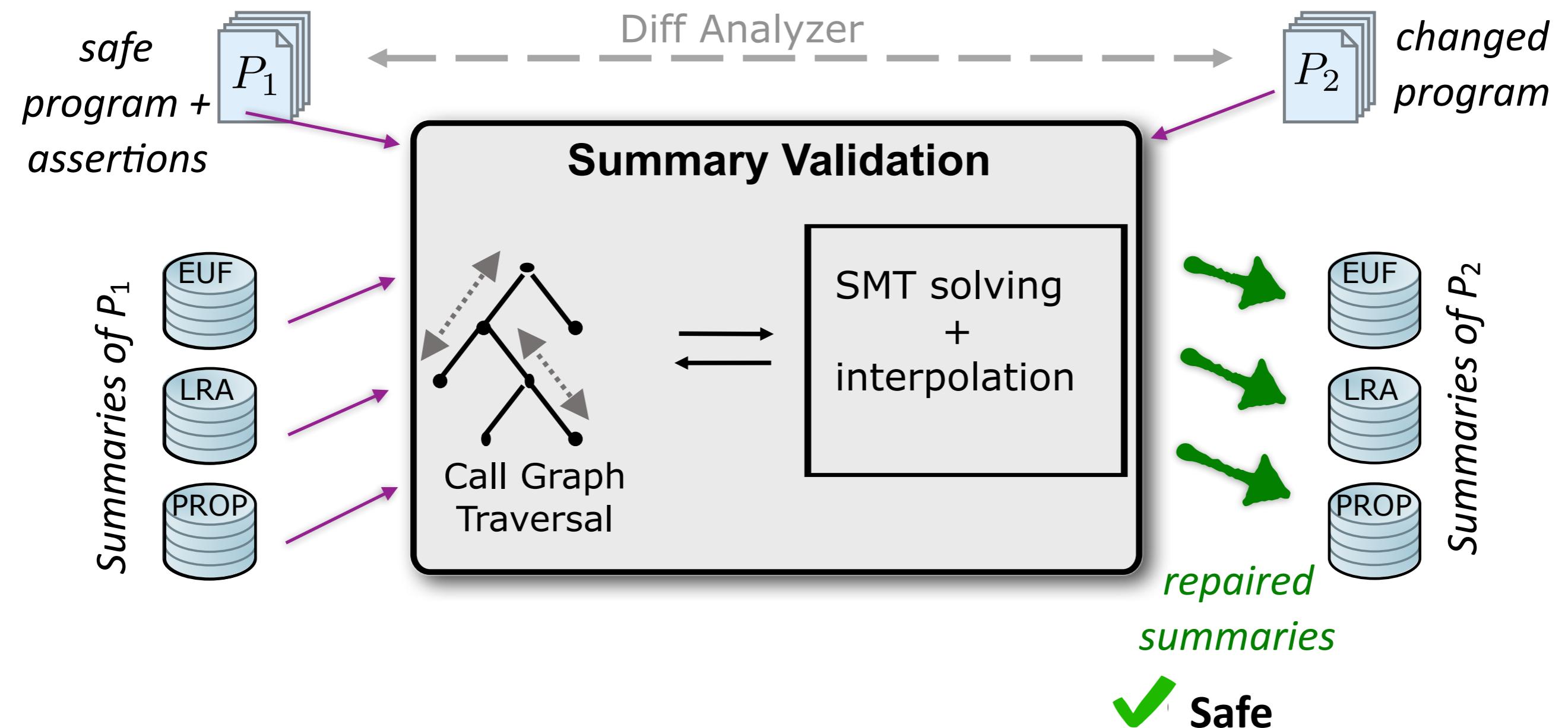
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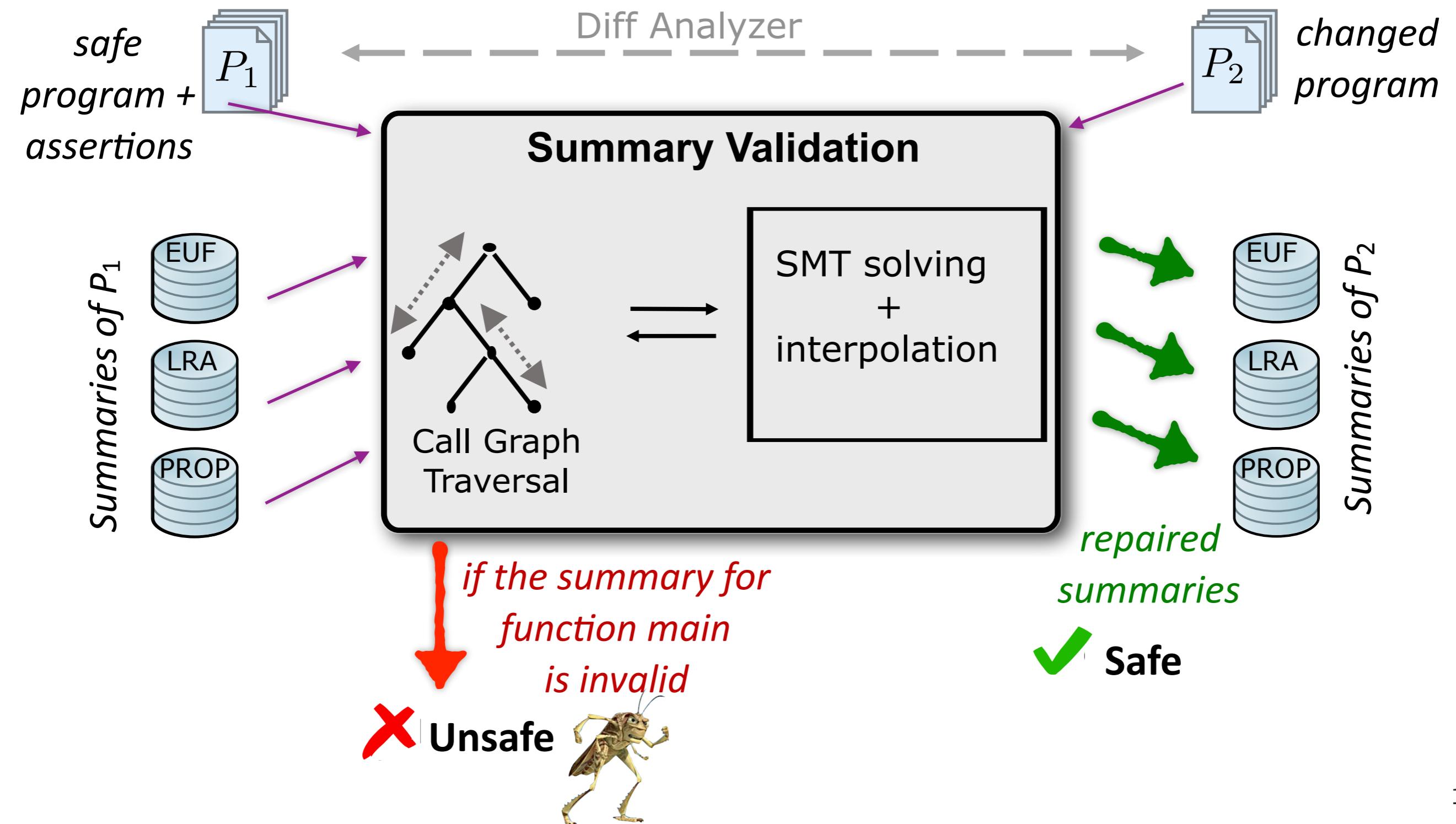
UpProver architecture



UpProver architecture



UpProver architecture



Underlying Technology of UpProver

- UpProver employs our SMT-solver **OpenSMT2** for SMT checks & interpolation. [Hyvärinen et al.]
 - <https://github.com/usi-verification-and-security/opensmt>
- UpProver uses the **CProver/CBMC** framework for symbolic pre-processing of C programs and the goto-program translation. [Kroening et al.]
 - <http://cprover.org>
- **NEW PART:**
Translation from goto-programs to various theories of SMT

Refinement

When summary validation fails:

- If over-approximative summaries in the sub-tree:
 - **Downward refinement**: Replace summaries by precise representation
- else **Upward refinement**

When SMT formula of the root function is **SAT** :

- Increase the precision by encoding to a more-precise theory

Evaluation

C Benchmarks

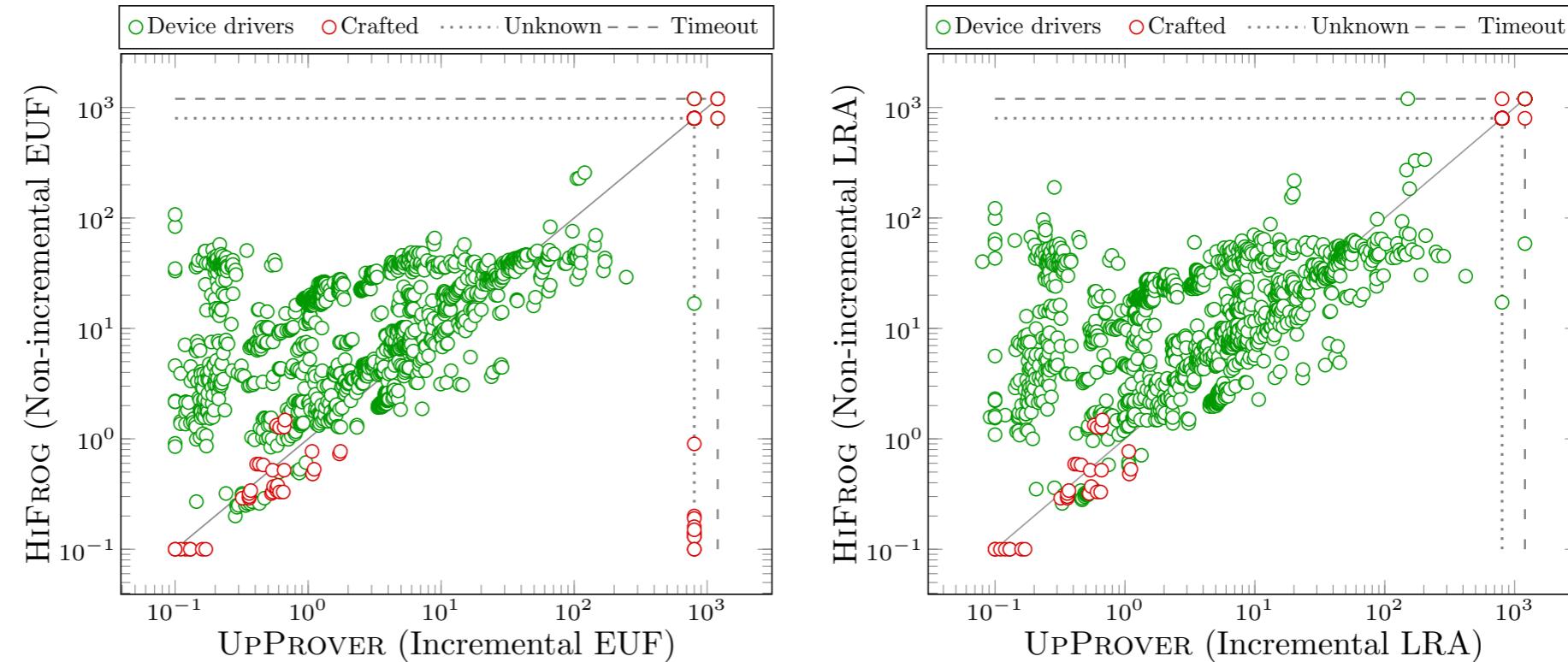
1700 pairs of revisions of Linux device drivers
90 pairs crafted benchmarks
LOC average: **16K**

Evaluation

C Benchmarks

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Impact of summary reuse

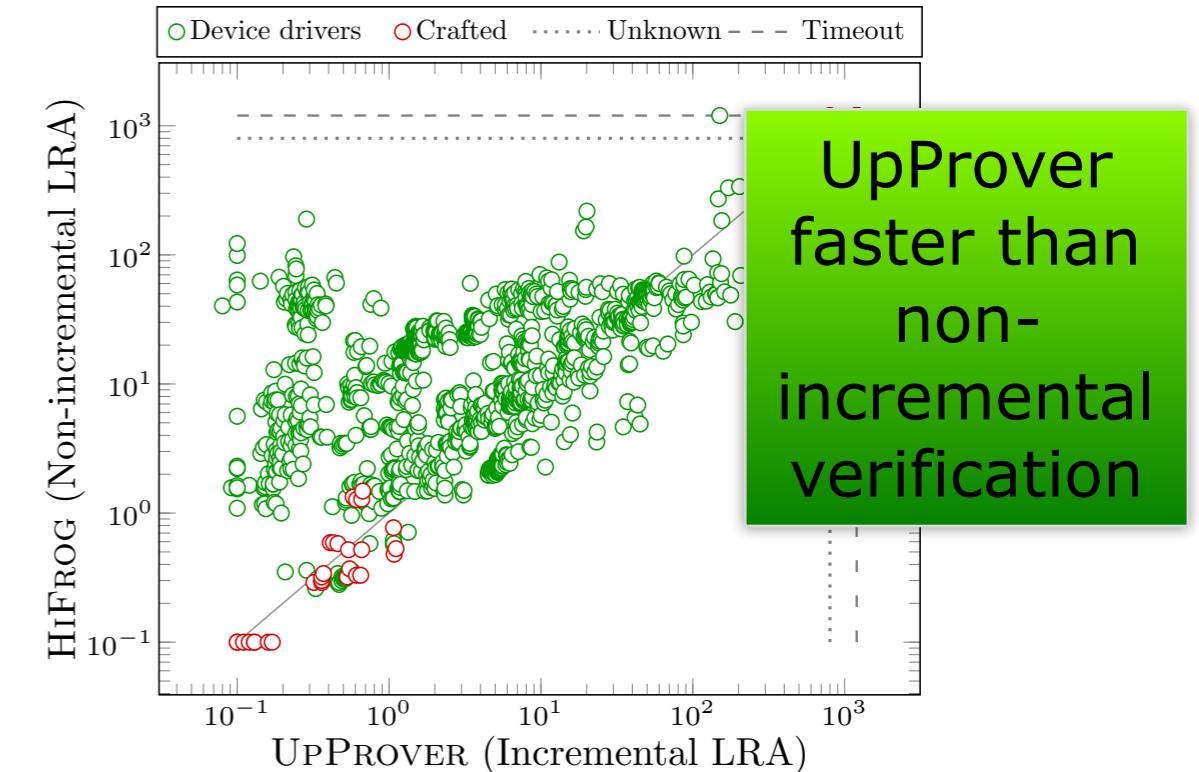
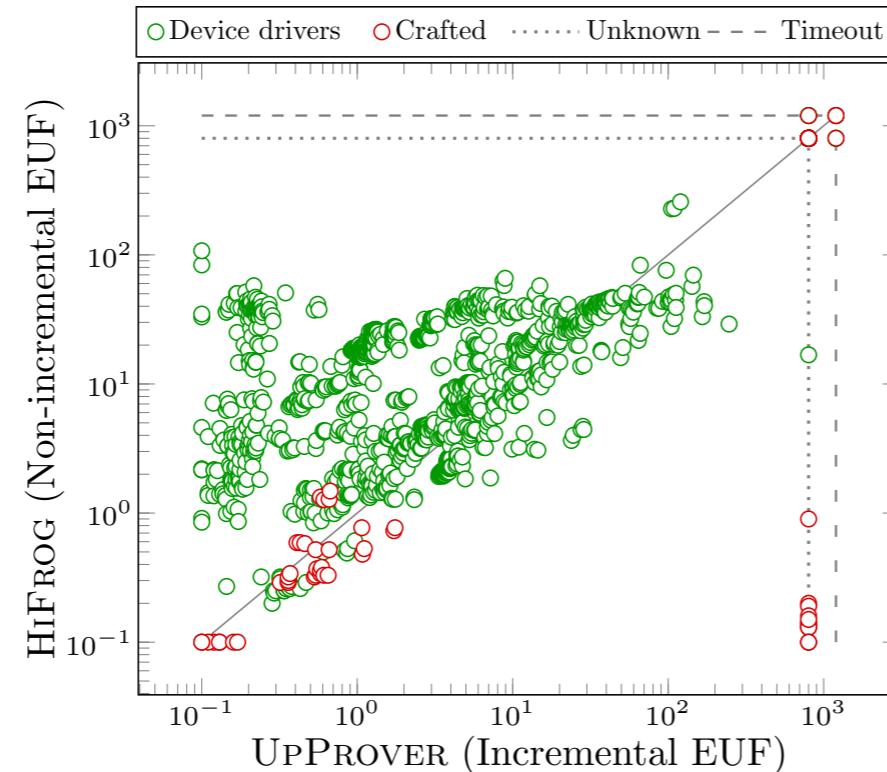


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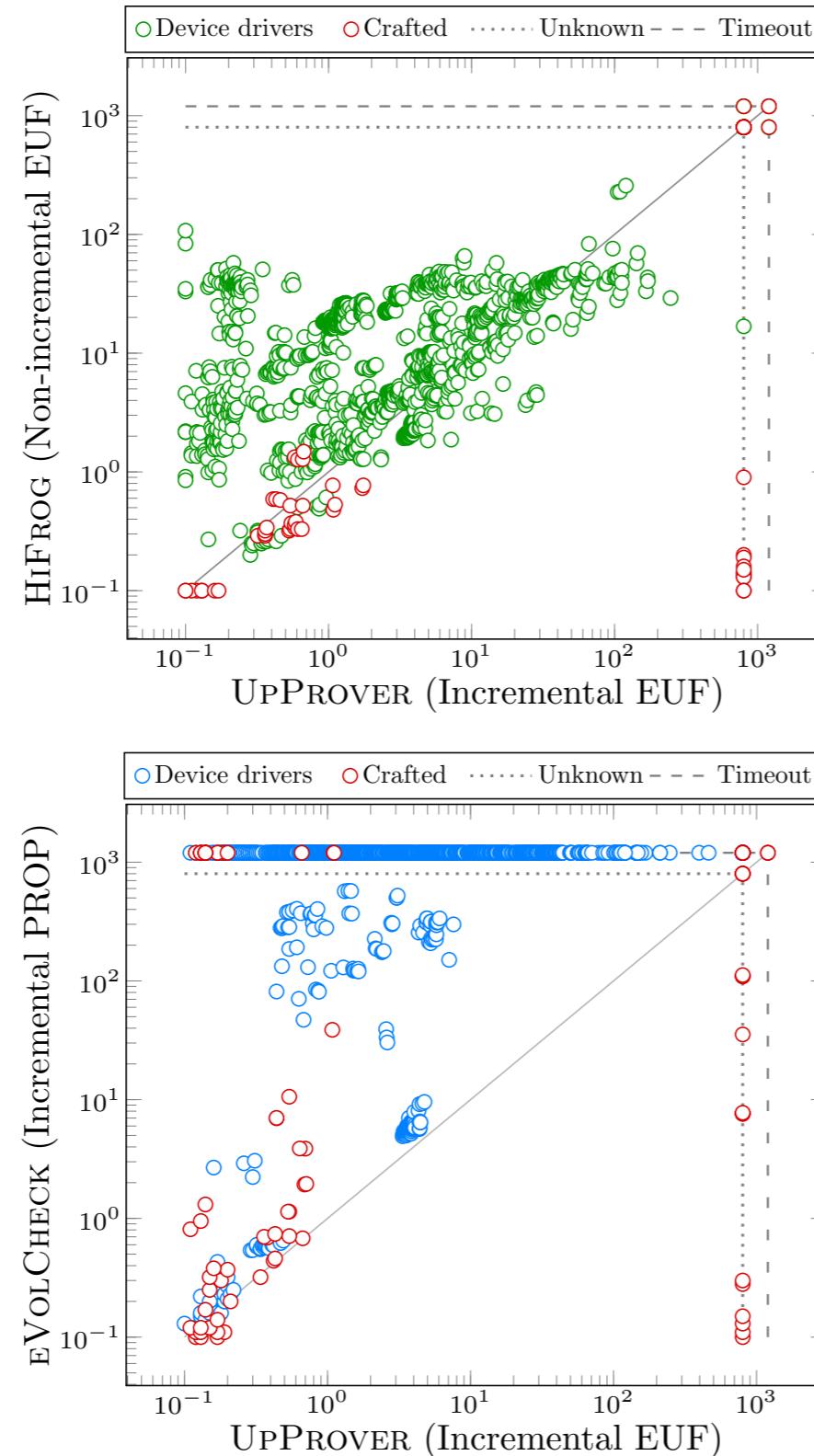
UpProver
faster than
non-
incremental
verification

Evaluation

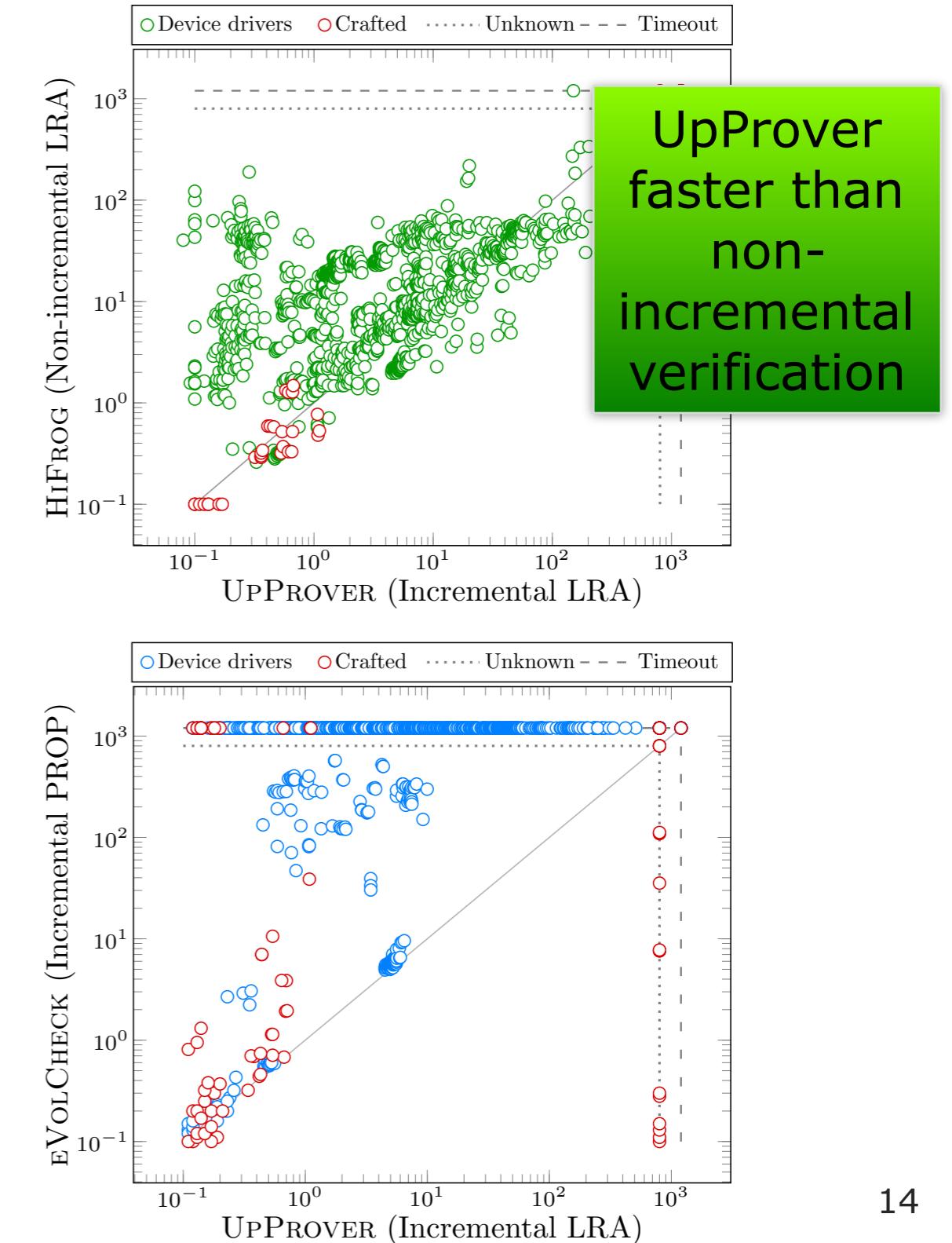
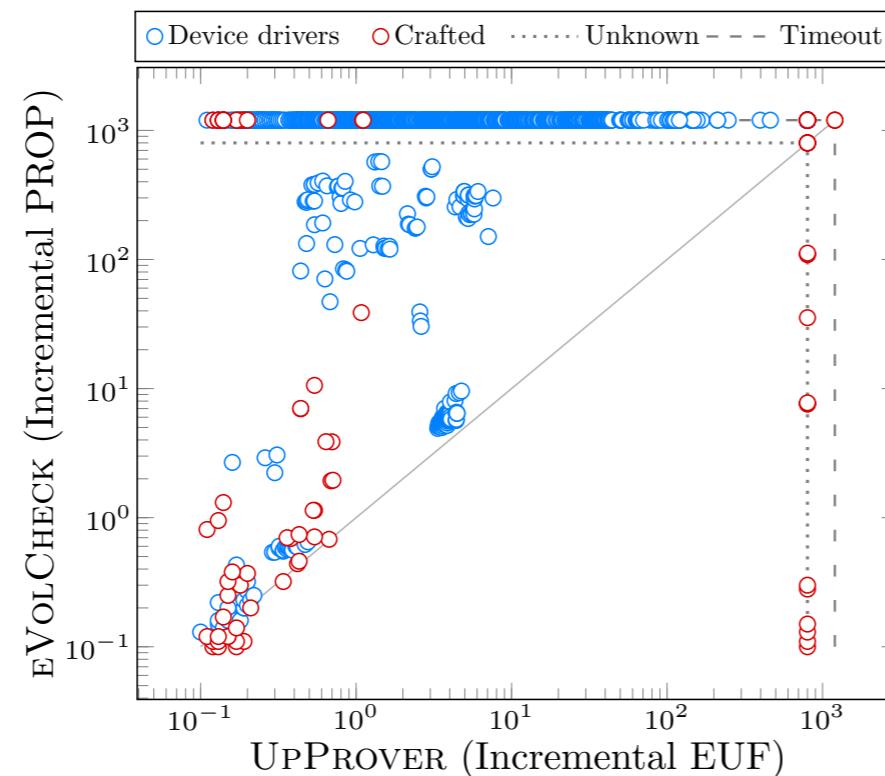
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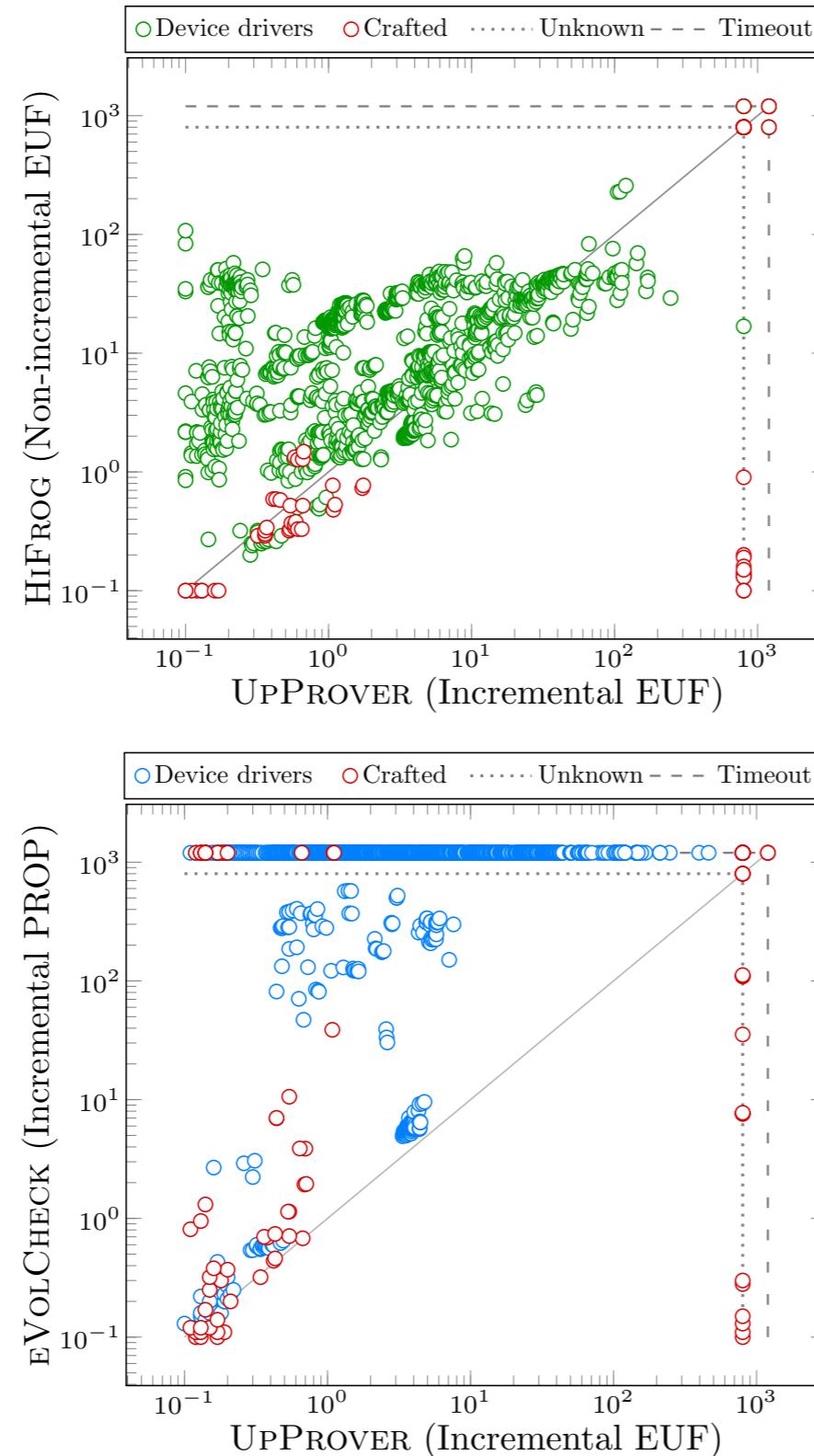


Evaluation

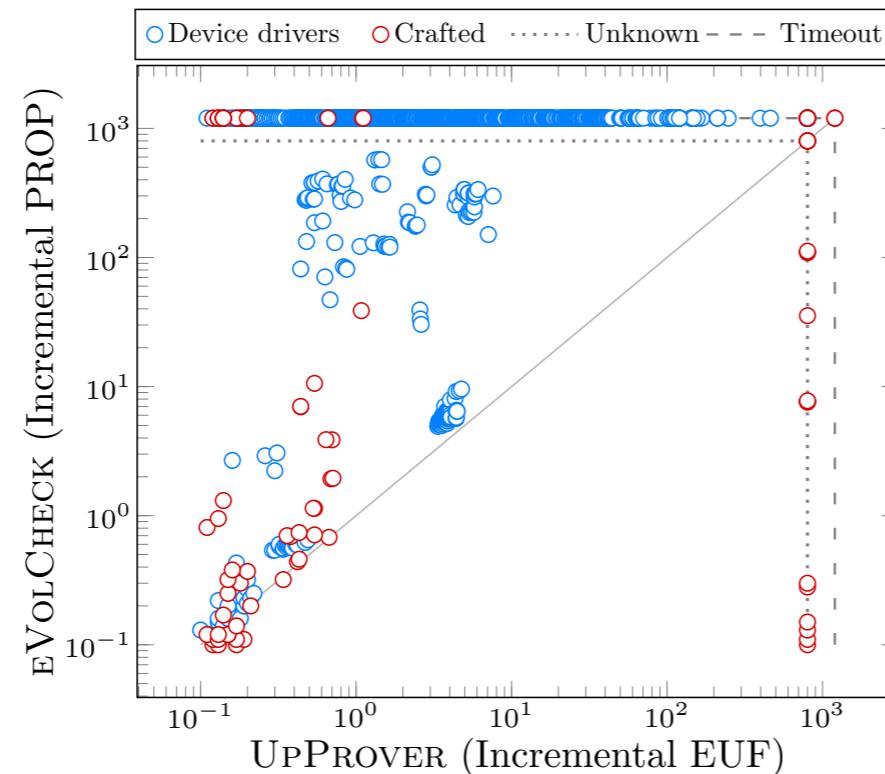
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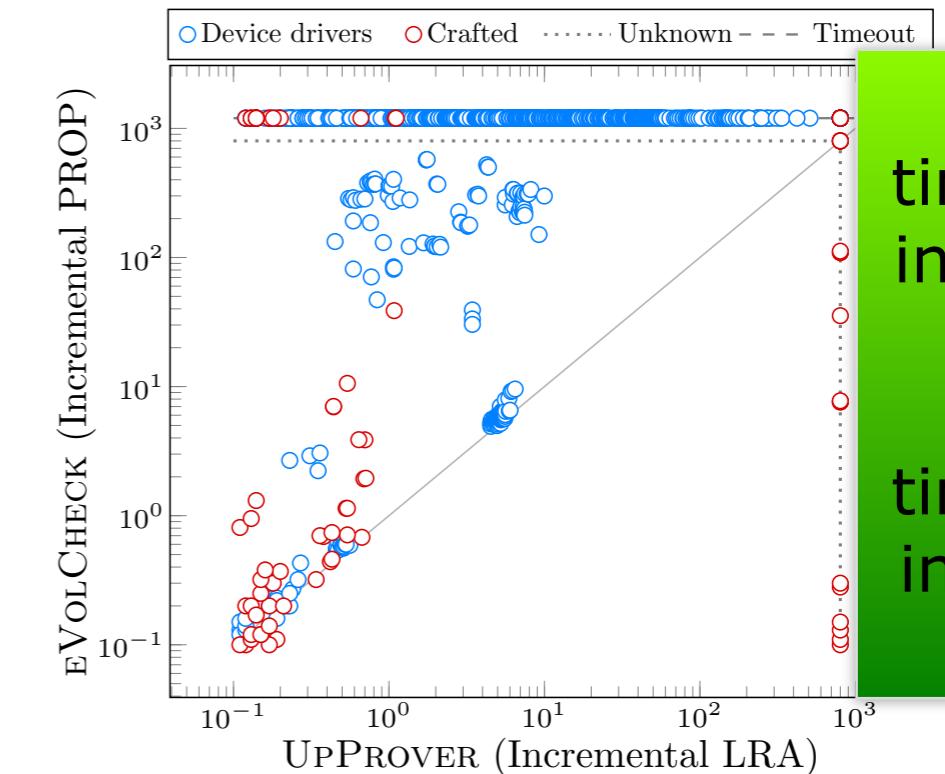
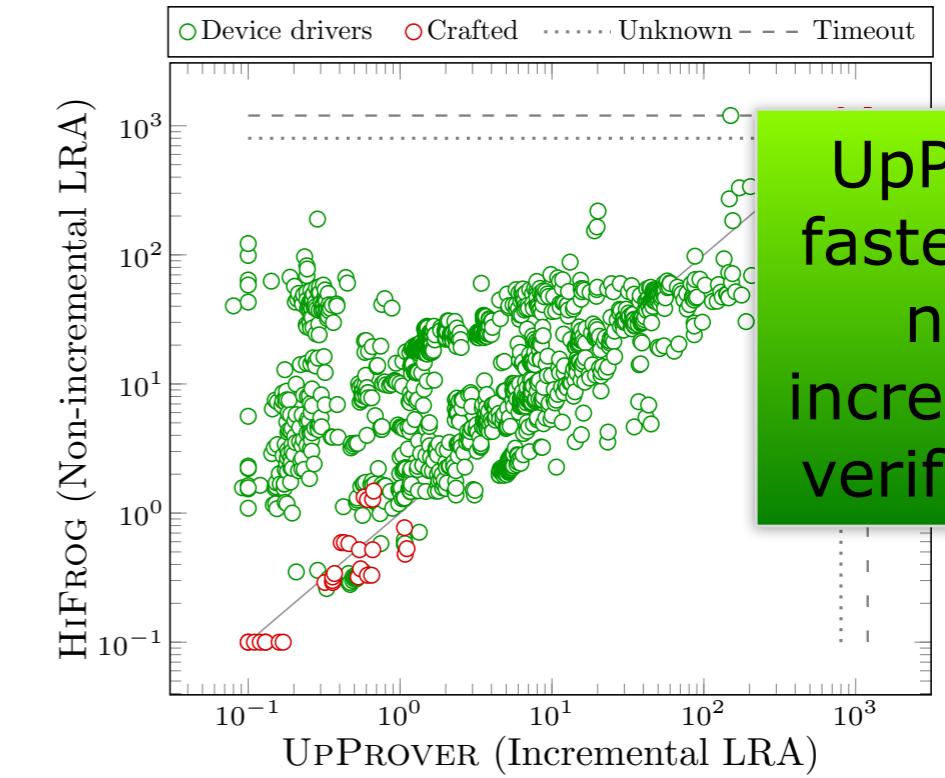
Impact of summary reuse



Impact of theory encoding



UpProver faster than non-incremental verification



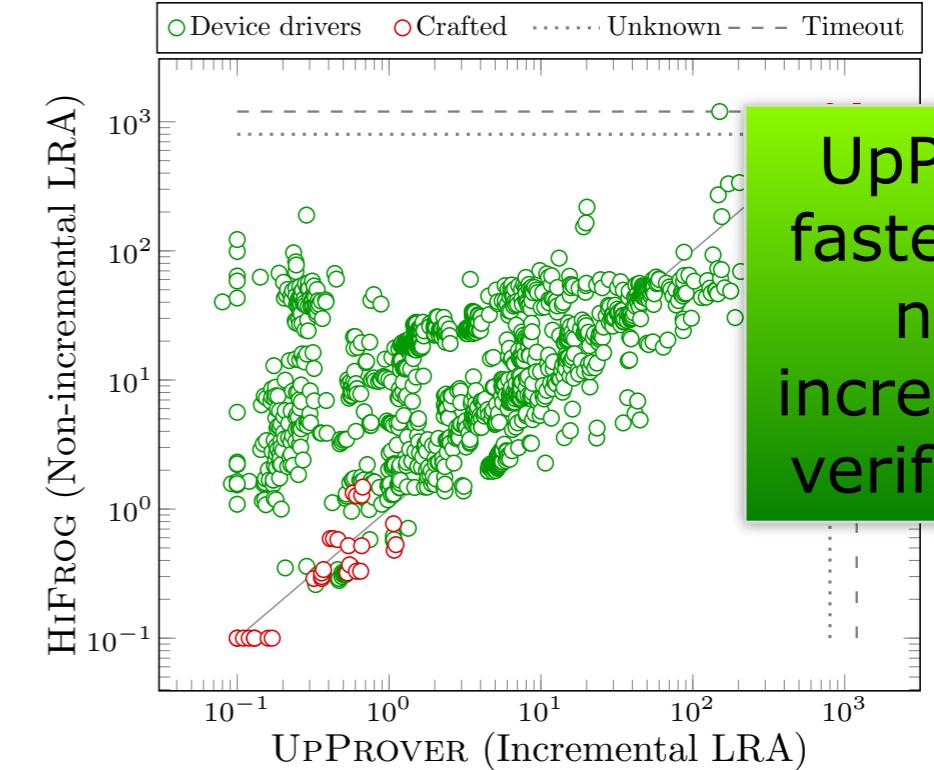
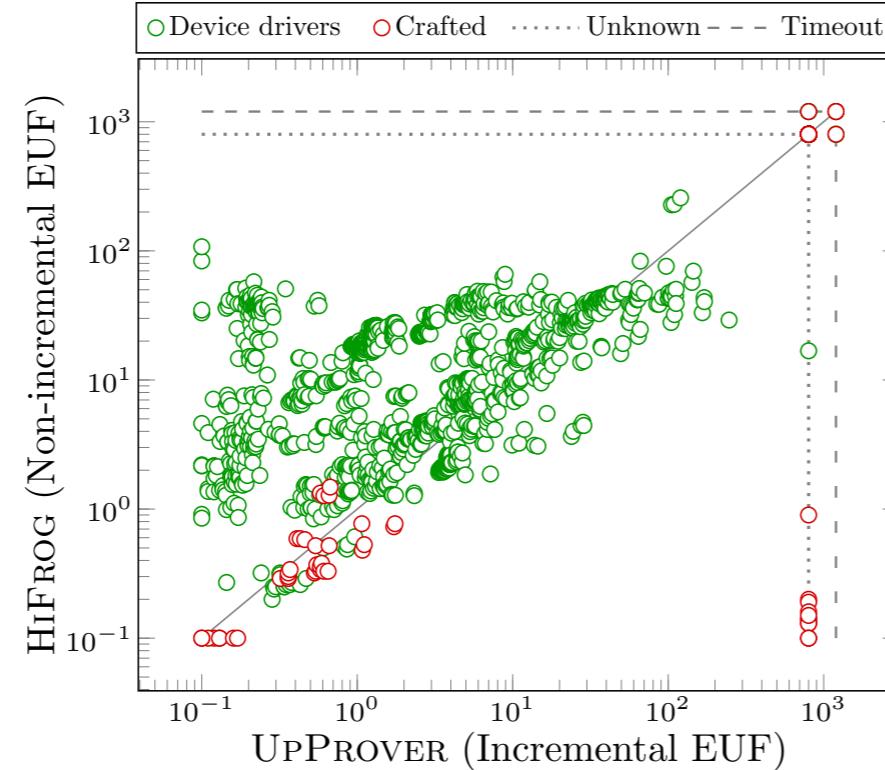
1328 timeouts in PROP
<15 timeouts in LRA/EUF

Evaluation

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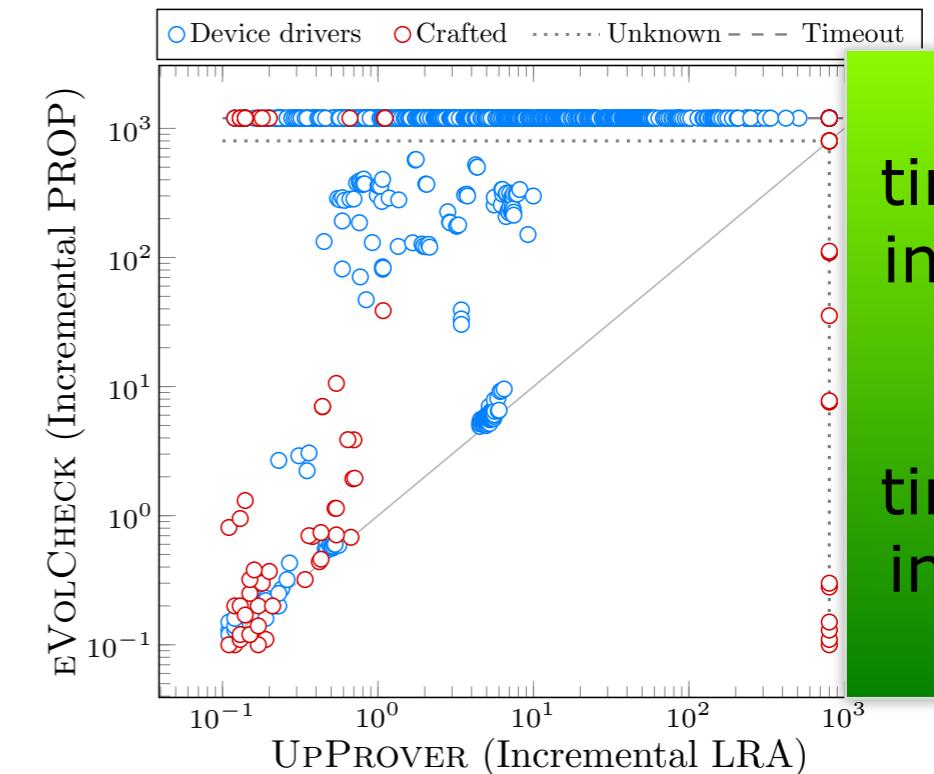
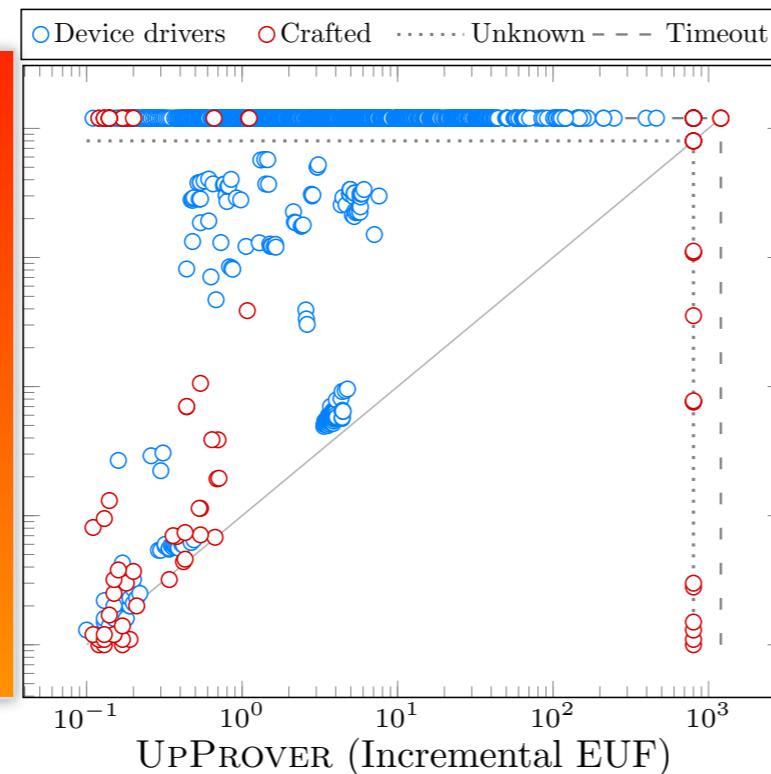
Impact of summary reuse



UpProver faster than non-incremental verification

Impact of theory encoding

0 unknown in **PROP**
76+86 unknown in **LRA/EUF**



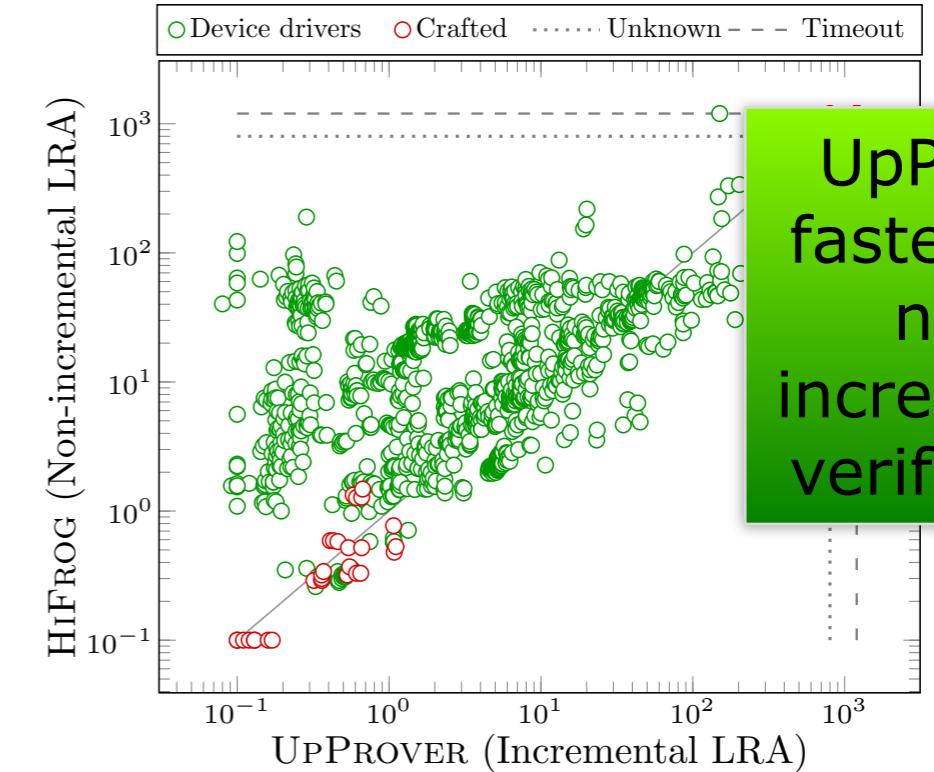
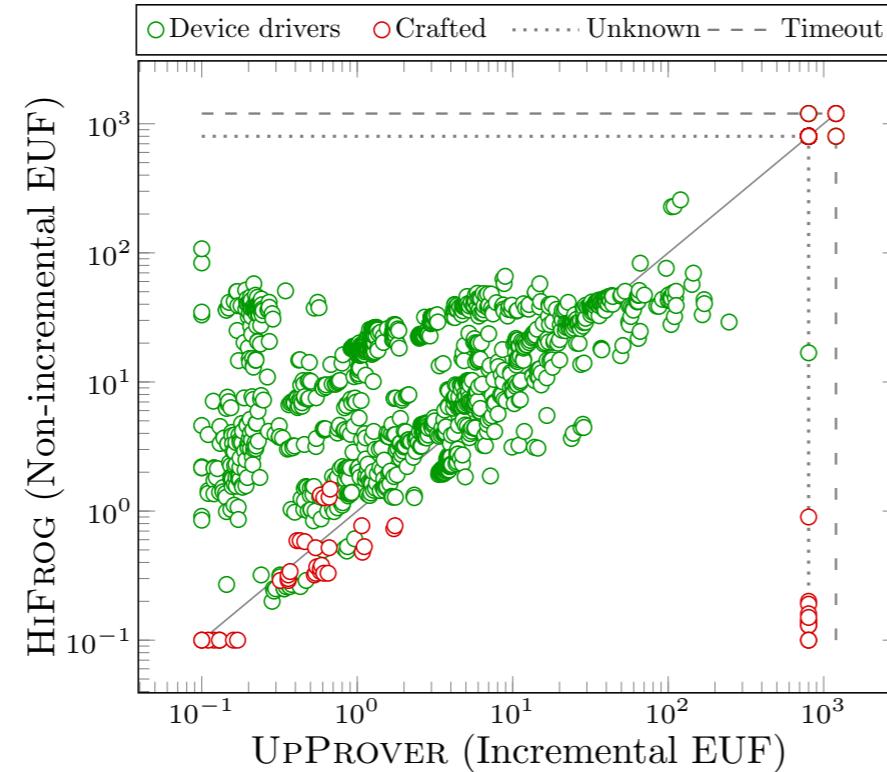
1328 timeouts in **PROP**
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Evaluation

C Benchmarks

1700 pairs of revisions of Linux device drivers
90 pairs crafted benchmarks
LOC average: 16K

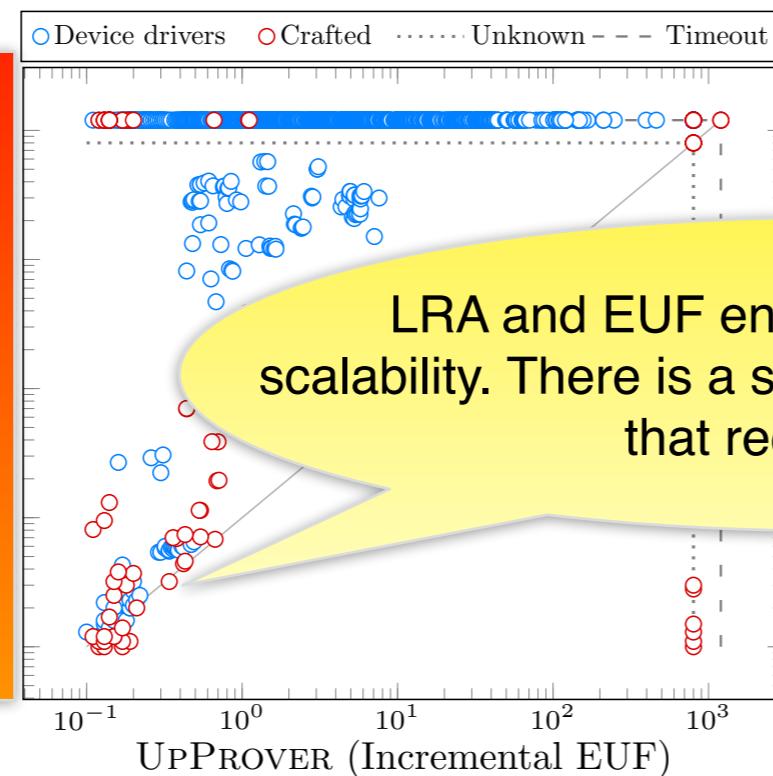
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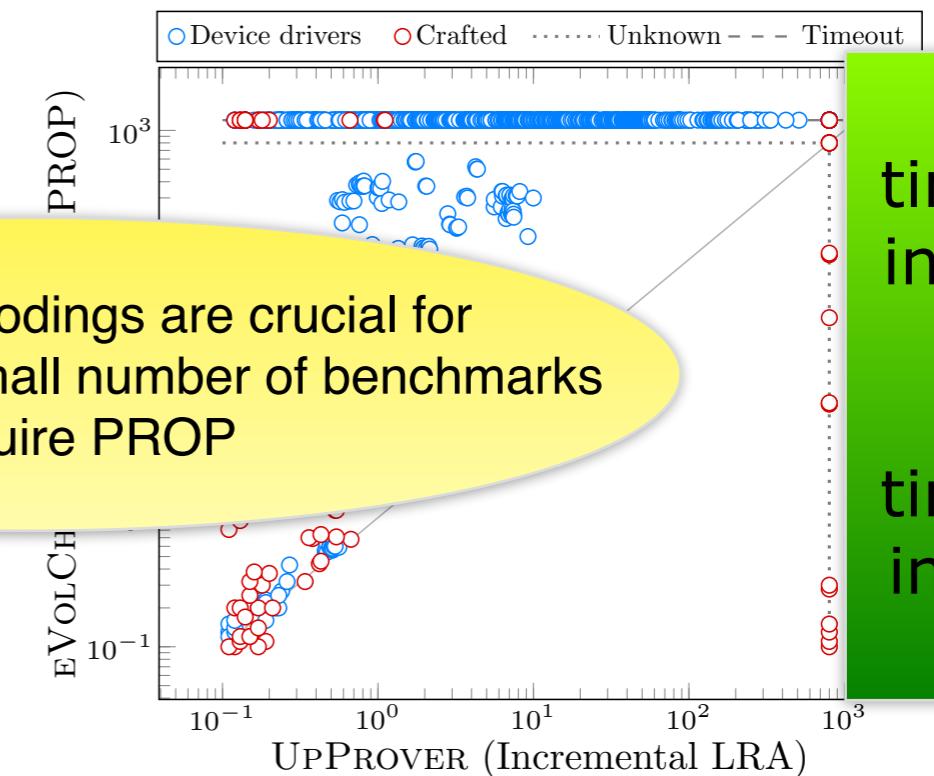
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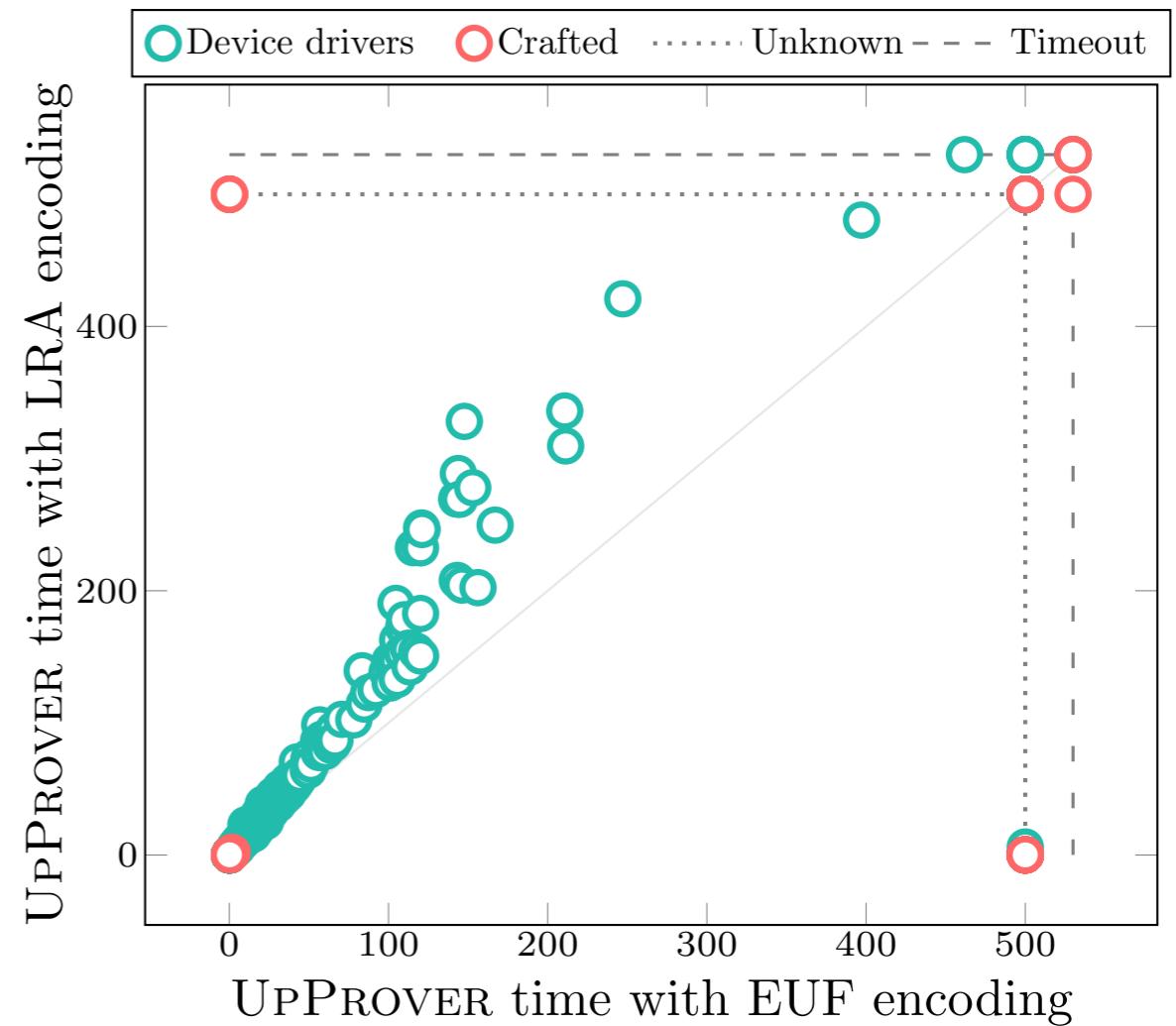
LRA and EUF encodings are crucial for scalability. There is a small number of benchmarks that require PROP



1328 timeouts in PROP
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LRA vs. EUF in UpProver

- LRA encoding vs. EUF has an almost 30% time overhead
 - Most likely because of the more expensive Simplex algorithm in LRA compared to EUF congruence algorithm
- ... but LRA is more precise than EUF

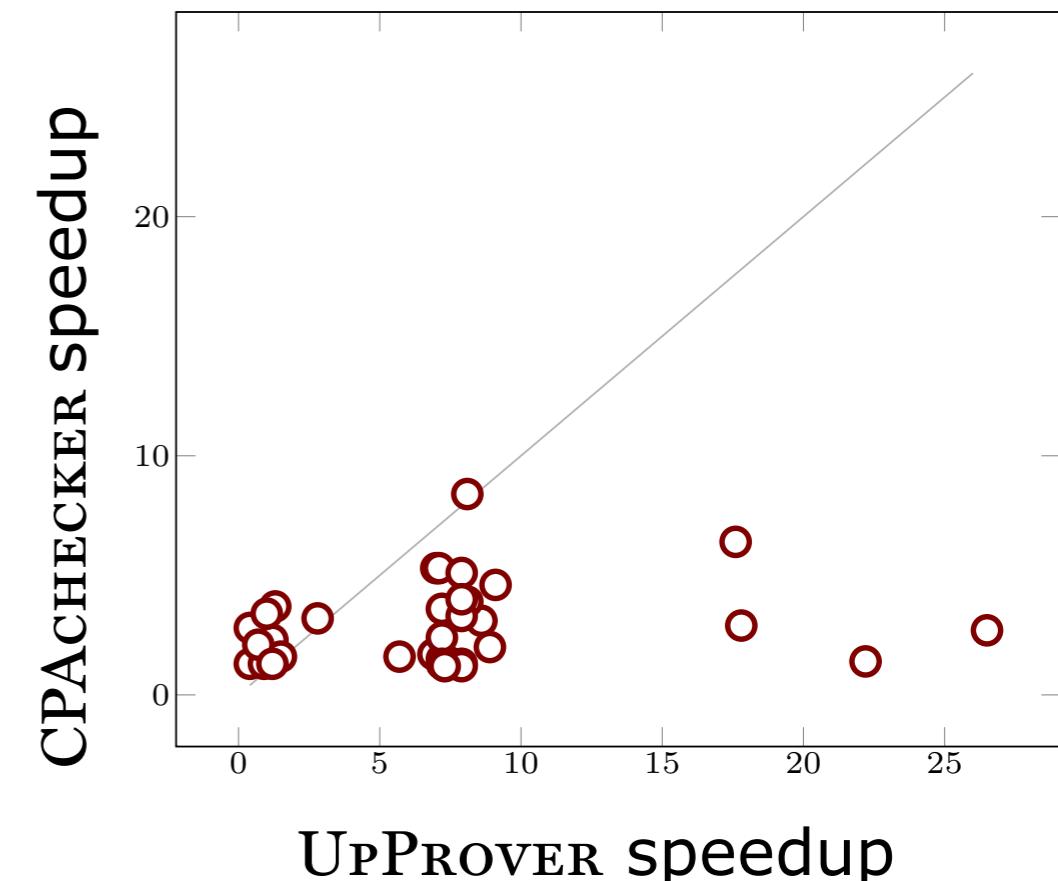


UpProver vs. CPAchecker

Summary reuse in UpPROVER vs precision reuse in CPAchecker

Speedup comparison for 34 categories
of device driver benchmarks with 903 revisions

Tool	Avg Speedup	Avg Slowdowns
UpPROVER	7.3 (30 categories)	0.6 (4 categories)
CPAchecker	2.9	no-slowdowns



Note that the approaches are orthogonal (BMC vs loop invariants), thus the comparison is not very accurate

Related Work

- **eVolCheck**: Incremental Upgrade Checker for C [Fedyukovich et. al TACAS'13]
- **Niagara**: Incremental CHC solver [Fedyukovich et. al. NFM'14, CAV'16]
- **HiFrog**: SMT-based function summarization for software verification [Alt et. al TACAS'17]
- **CPAchecker**: Precision reuse for efficient regression verification [Beyer et. al 2013]
- **ModDiff** (based on CProver): Modular Demand-Driven Analysis of Semantic Difference for Program Versions [Trostanetski et. al 2017]

Future Work

- ▶ Extend the tool to handle summaries across different theories, possibly by allowing checks for the tree-interpolation property on-the-fly

Conclusion

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<http://verify.inf.usi.ch/upprover>